



Magnetic Components Design

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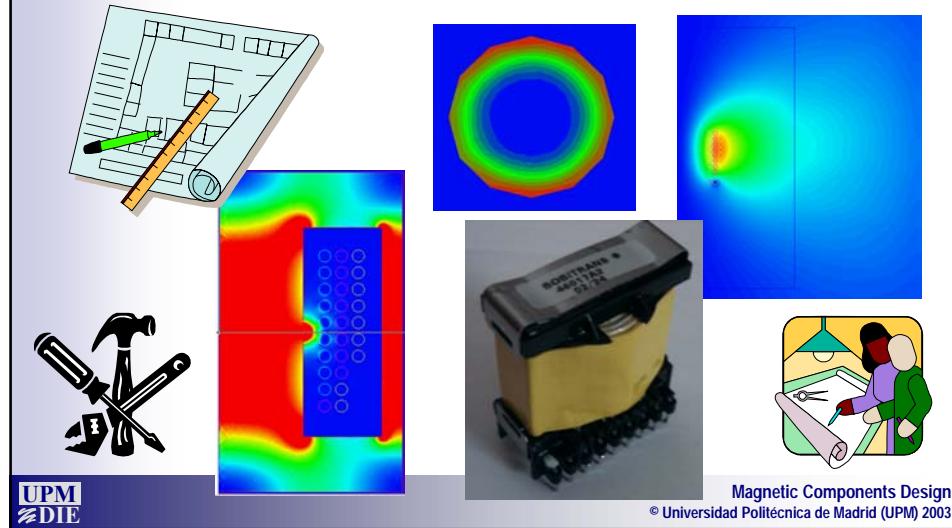
Seminar Contents

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Basic Concepts



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Basic Magnetic Theory

AMPERE'S LAW

$$\oint \mathbf{H} d\mathbf{l} = ni$$

FARADAY'S LAW

$$V(t) = n \frac{d\Phi}{dt}$$

$$\mathbf{B} = \mu \mathbf{H}$$

$$\Phi = BA$$

$$\mu = \mu_r \mu_0$$

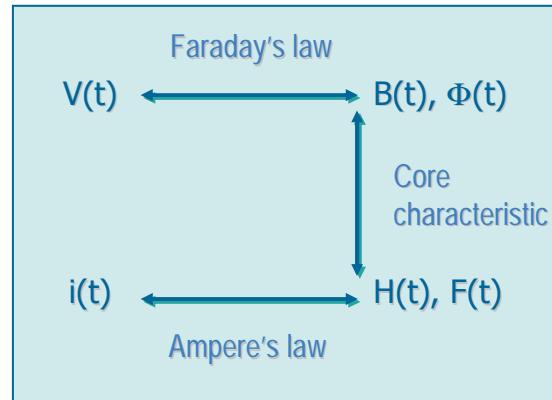
- H: Magnetic field
Φ: Magnetic flux
B: Magnetic flux density
A: Area
V(t): Voltage
i: Current
dl: Vector lenght
 μ : Permeability
 μ_0 : Air permeability
 μ_r : Relative permeability
n: Number of turns
F(t): Electromagnetic force

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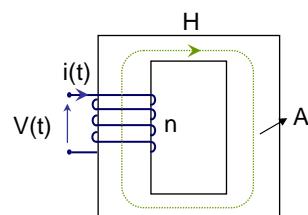
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Basic Magnetic Theory



Basic Magnetic Theory



$$V(t) = nA \frac{dB(t)}{dt}$$

$$H(t)l = ni(t)$$

$$V(t) = nA\mu \frac{dH(t)}{dt}$$

$$V(t) = \frac{n^2 A}{l} \mu \frac{di(t)}{dt}$$

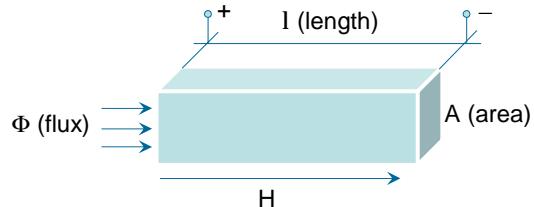
$$L = \frac{\mu n^2 A}{l}$$

$$V(t) = L \frac{di(t)}{dt}$$



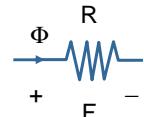
Basic Magnetic Theory

Magnetic Circuits

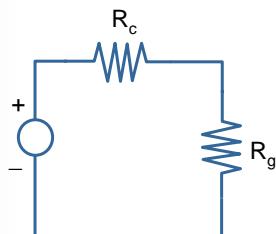
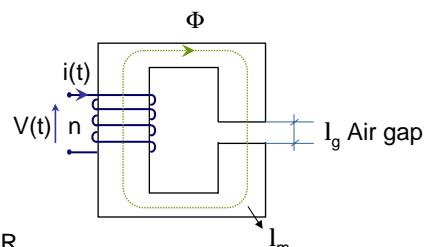


$$F = HI = \frac{l}{\mu A} \Phi$$

$$F = \Phi R \Rightarrow R = \frac{1}{\mu A} \quad (\text{Reluctance})$$



Basic Magnetic Theory



$$ni(t) = \Phi(R_c + R_g)$$



Basic Magnetic Theory

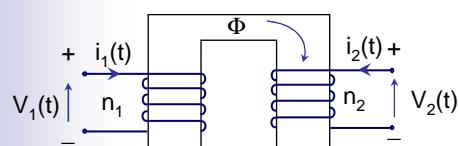
$$\left. \begin{aligned} V(t) &= n \frac{d\Phi}{dt} \\ ni(t) &= \Phi(R_c + R_g) \end{aligned} \right\} V(t) = \frac{n^2}{R_c + R_g} d \frac{i(t)}{dt}$$

$$L = \frac{n^2}{R_c + R_g}$$



Basic Magnetic Theory

Transformer



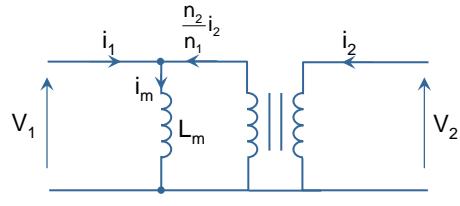
$$\left. \begin{aligned} R &= \frac{l_m}{\mu A} \\ n_1 i_1 + n_2 i_2 &= \Phi R \\ V_1 &= n_1 \frac{d\Phi}{dt} \\ V_2 &= n_2 \frac{d\Phi}{dt} \end{aligned} \right\} \frac{d\Phi}{dt} = \frac{V_1}{n_1} = \frac{V_2}{n_2}$$



Basic Magnetic Theory

$$V_1 = \frac{n_1^2}{R} \frac{d}{dt} \left[i_1 + \frac{n_2}{n_1} i_2 \right]$$

$$V_1 = L_m \frac{di_m}{dt}$$



$$L_m = \frac{n_1^2}{R}; \quad i_m = i_1 + \frac{n_2}{n_1} i_2$$



Basic Concepts

There are many Applications of Magnetic components

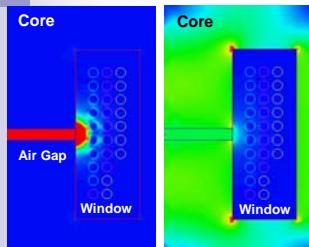
- ✓ Galvanic Isolation
- ✓ Adjust Voltage Levels
- ✓ Filters
- ✓ Resonant Inductors
- ✓ Measurements for Feedback and Protections
- ✓ Pulse Transformers
- ✓ ...

But basically, they produce

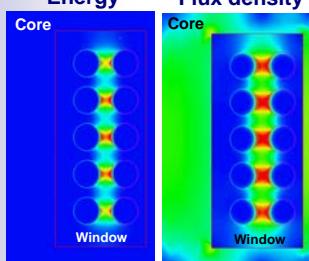
- ✓ Energy Storage
- ✓ Energy Transfer
- ✓ Losses



Magnetic Energy

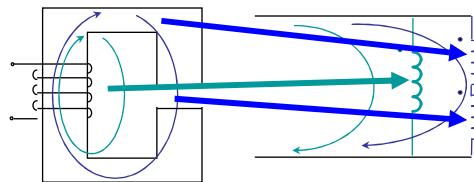


Energy



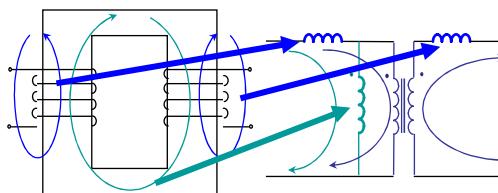
Flux density

Inductors



Each inductance models the
“magnetic energy storage”
In each different zone

Transformers

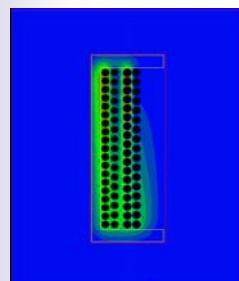


Magnetic Components Design

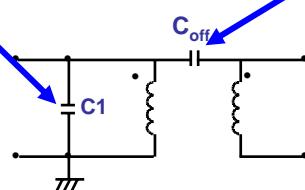
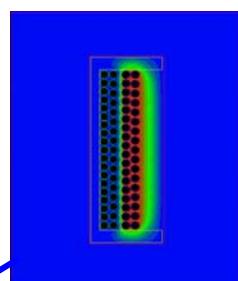
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Electric Energy



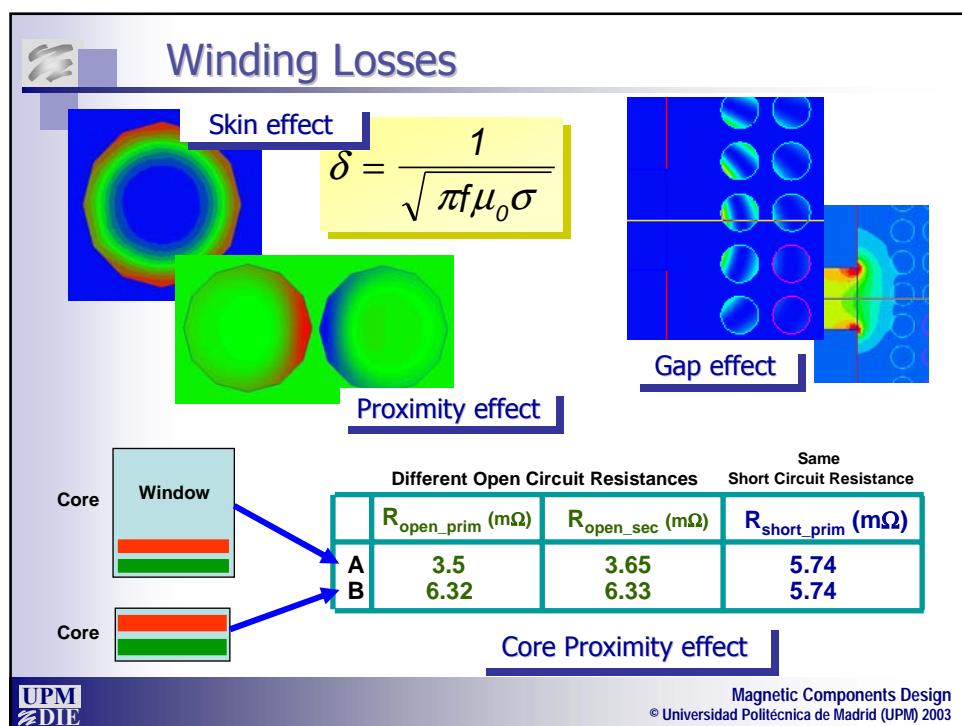
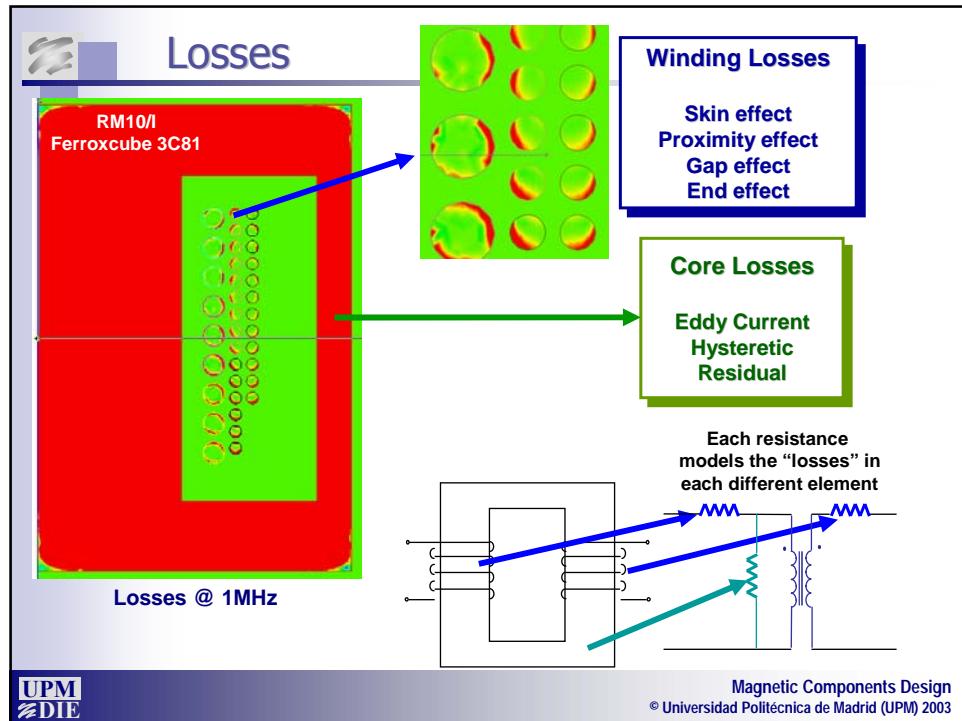
Each capacitance models the
“electric energy storage”



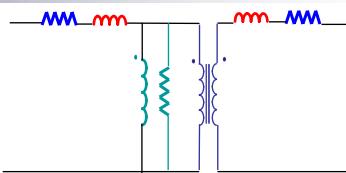
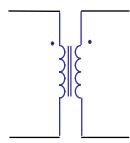
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Ideal and Real Components



➤ Ideal transformer:

$$\frac{d\phi}{dt} = \frac{v_1}{n_1} = \frac{v_2}{n_2} = \dots = \frac{v_p}{n_p}$$

$$n_1 \cdot i_1 = n_2 \cdot i_2$$

No energy storage !!

No losses !!

➤ Real transformer :

✓ Common energy:

$$L_{mag,i} = \frac{n_i^2}{R}$$

$$\sum ni = \Phi \cdot R$$

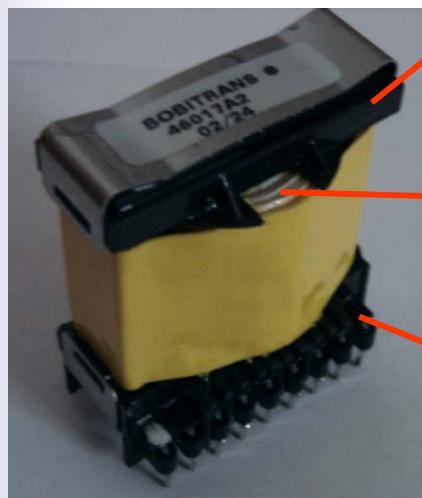
From any winding

✓ Self energy

✓ Conductor losses

Notice the difference between
“transferred” and “stored” energy

Magnetic Component Elements



Core

- Flux Path
- Energy storage

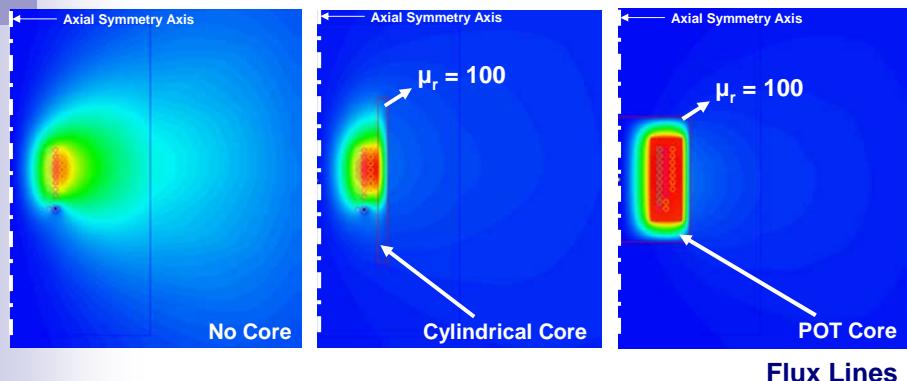
Windings

- Electrical terminals
- Current path

Bobbin

- Windings holder

The Role of the Core I



Flux Lines

The Core helps to create a flux path

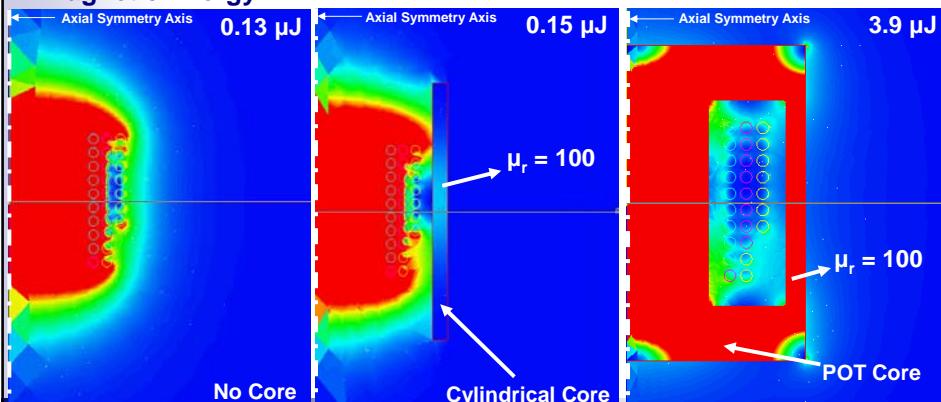
*Additionally the core determines the energy and inductance
Unfortunately, the core also produces losses*

The Role of the Core II

$$\text{Reluctance} \quad \mathfrak{R} = \frac{1}{\mu} \cdot \frac{\text{length}}{\text{Area}}$$

$$L = \mu_0 \cdot \mu_r \cdot \frac{\text{Area}}{\text{Length}} \cdot n^2$$

Magnetic Energy

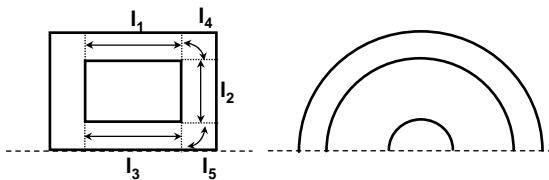


The Effective Values of the Core

Effective Values



Example: POT Core



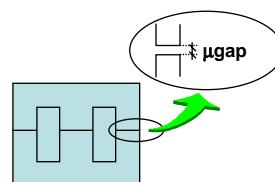
$$L = \mu_0 \cdot \mu_r \cdot \frac{\text{Area}}{\text{Length}} n^2$$

$$A_e = \frac{C_1}{C_2}; \quad V_e = \frac{C_1^3}{C_2^2}; \quad I_e = \frac{C_1^2}{C_2}$$

$$C_1 = \sum_1^5 \frac{l_i}{A_i} mm^{-1} \quad C_2 = \sum_1^5 \frac{l_i}{A_i^2} mm^{-3}$$

The Tolerances of the Core

GRADE	A_L (nH)	μ_e	AIR GAP (μm)
3B8 sup	160 $\pm 3\%$	≈ 59	≈ 900
	250 $\pm 3\%$	≈ 92	≈ 500
	315 $\pm 3\%$	≈ 116	≈ 400
	400 $\pm 3\%$	≈ 147	≈ 300
	630 $\pm 3\%$	≈ 232	≈ 150
	4950 $\pm 25\%$	≈ 1820	≈ 0



μ_e (and A_L) depends on the "micro-gap"
(2.5 μm or 100 mils each union) because of
mechanization process

The Core Choices

Shapes
RM, POT, EE, EI, PQ, TOROIDS...

- Effective values
- Magnetic coupling
- Heat transfer
- Unit Cost
- Manufacturing Cost

Materials
3F3, 3C85, 3C90, N67, N47...

- Core losses
- Permeability and Reluctance
- Conductivity
- Saturation flux density

$$L = \mu_o \cdot \mu_r \cdot \frac{\text{Area}}{\text{Length}}$$

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The Role of the Gap

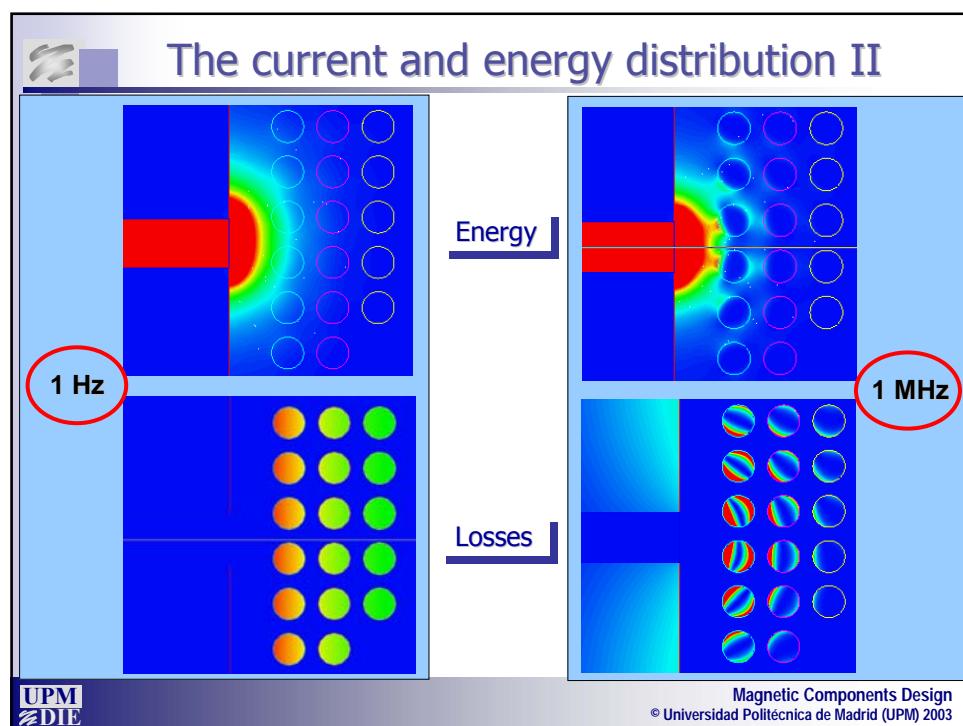
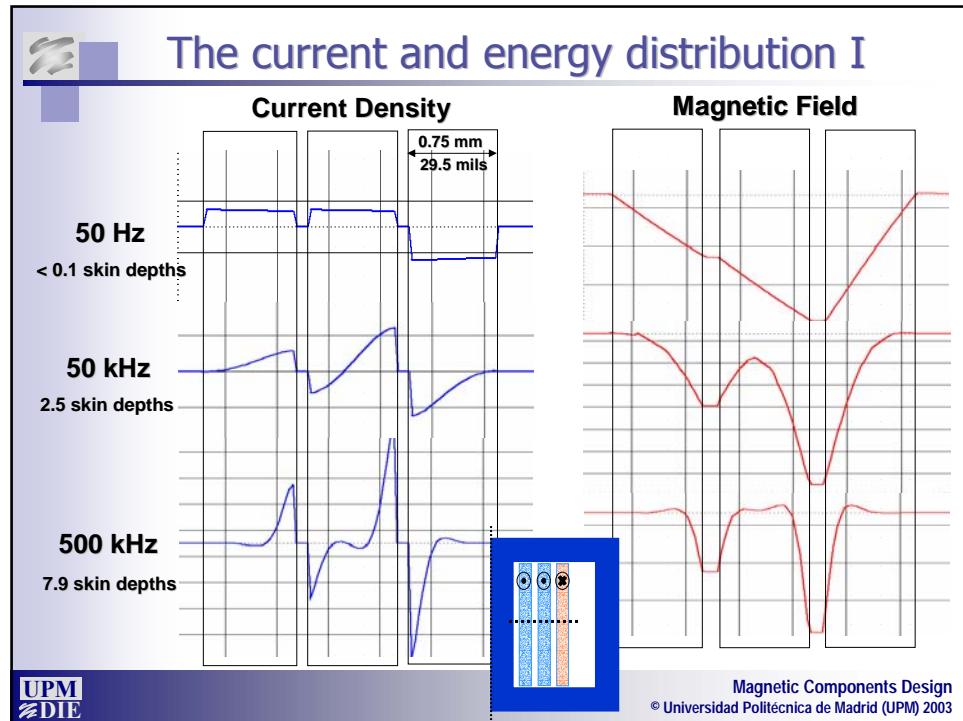
- Adjust the reluctance value
- Adjust the energy storage
- Avoid saturation

Gap Type	Core Losses ($\mu\text{W}/\text{m}^2$)	Energy Storage (μJ)
No Gap	~1000	89 μJ
10 μm Air Gap	~10000	238 μH
50 μm Air Gap	~100000	43 μJ , 138 μH
100 μm Air Gap	~1000000	14 μJ , 52 μH
150 μm Air Gap	~10000000	8 μJ , 30 μH , 6 μJ , 21 μH

Energy

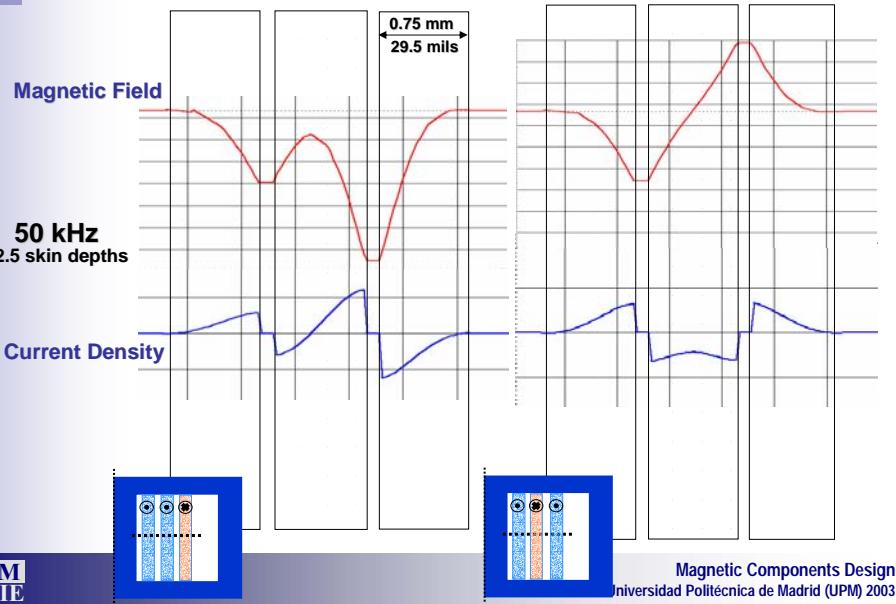
Ferrite Core

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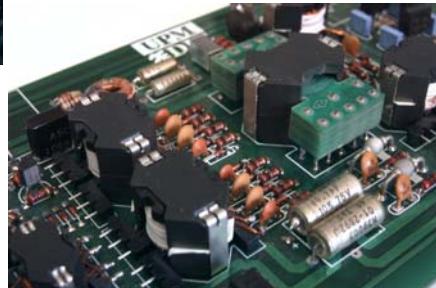




Interleaving Application



Design



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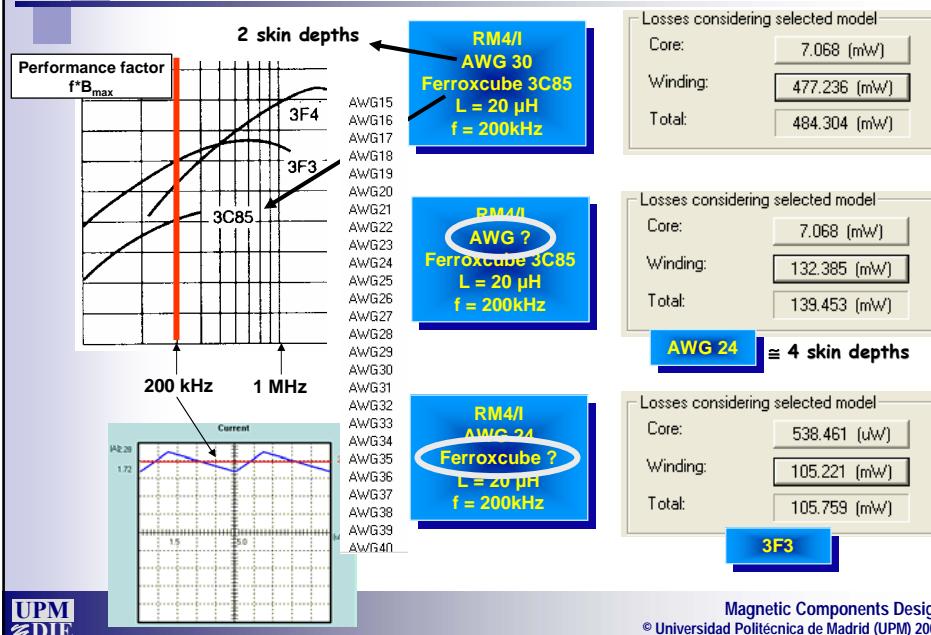


Selection of Constructive Elements

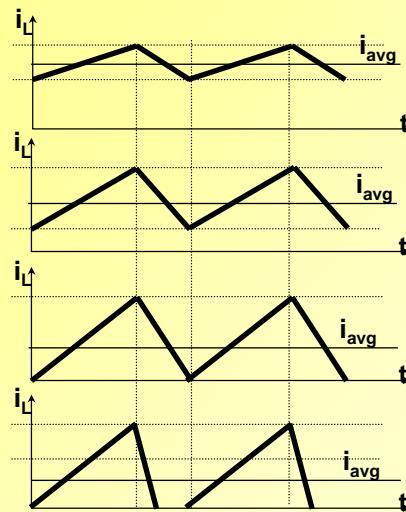
1. CORE SHAPE → Depends on the application (see data books)
2. CORE SIZE → Depends on the power ("area product" or data books)
3. CORE MATERIAL → Depends on the "frequency" (see data books)
4. CONDUCTOR TYPE → Depends on the "frequency" (skin depth)
 - Solid wire: low frequency
 - Litz wire and foils: high frequency
5. CONDUCTOR AREA → Depends on the optimum losses



Example of selection of elements



The “effective frequency” concept



Same frequency?
Yes

Same “effective frequency”?
No

Affects the selection of:

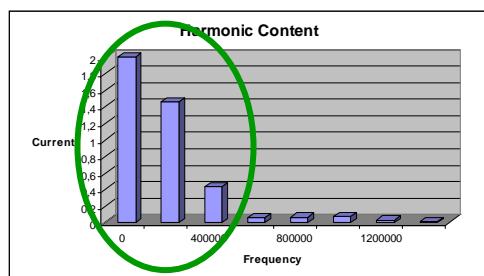
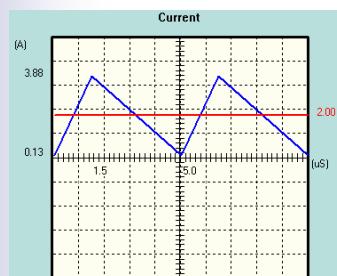
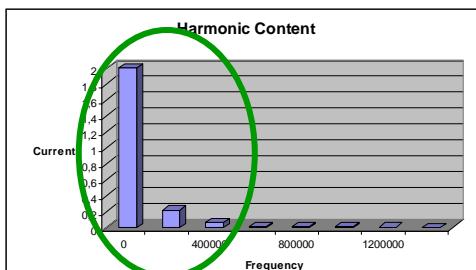
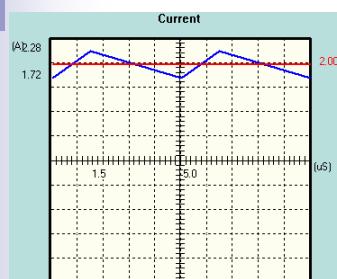
CORE MATERIAL

CONDUCTOR TYPE

CONDUCTOR AREA



The “effective frequency” concept



Example (Effective Frequency)

Vpos = 7.5 V; Vneg = 3.21 V; Switch. Freq = 200 kHz; Iavg = 2 A; Duty = 30%

Core shape and size: RM5/I
Wire gauge: AWG28 (370 µm or 14.5 mils diameter)

Core RM5/I:

- Iavg = 2 A**
- L = 100 µH; Ripple = 112.5 mA**
- Ripple = 5.6% Iavg**

Core RM5/I (Ferrox cube 3F35):

- Iavg = 2 A**
- L = 10 µH; Ripple = 1.125 A**
- Ripple = 56% Iavg**

Core 3F35 (Ferrite):
Losses = 785 mW (32 turns)

Core 2P90 (Iron Powder):
Losses = 577 mW (16 turns)

Core 3F35 (Ferrite):
Losses = 89 mW (4 turns)

Core 2P90 (Iron Powder):
Losses = 371 mW (16 turns)

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Inductors

Calculation of Inductance

The graph shows the current i_L and voltage v_L over time t . The current i_L is a sawtooth waveform with a maximum value i_{max} and a minimum value i_{min} . The voltage v_L is a square wave that is high during the time interval t_1 and low during the time interval t_2 .

Δi (ripple) is indicated as the difference between i_{max} and i_{min} .

$V_i = L \frac{\Delta i}{t_1}$

$L = \frac{V_i \cdot t_1}{\Delta i}$

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Inductors

Calculation of initial number of turns

The minimum number of turns should be calculated in order to keep flux density under the saturation value

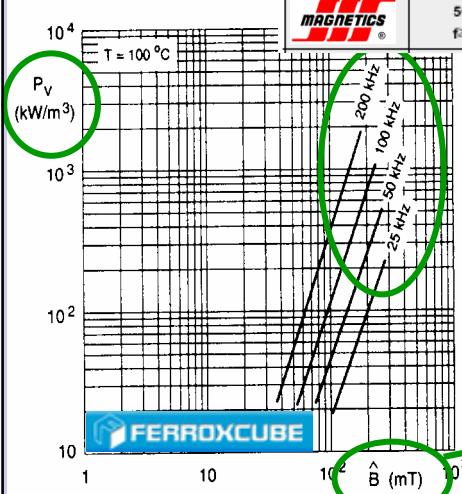
$$L \frac{\Delta i}{\Delta t} = N \frac{\Delta \Phi}{\Delta t} \rightarrow L \Delta i = N \cdot A_e \cdot \Delta B \rightarrow$$

$$\rightarrow L \cdot i_{max} = N \cdot A_e \cdot B_{max} \rightarrow N = \frac{L \cdot i_{max}}{A_e \cdot B_{max}}$$

This number of turns ensures that the inductor will not be saturated

Core Losses Calculation

Material	Frequency	a	c	d
K	f<500 kHz	0.0530	1.60	3.15
MAGNETICS	500 kHz < f < 1 MHz	0.00113	2.19	3.10
	f > 1 MHz	1.77*10 ⁻⁹	4.13	2.98



Steinmetz Equation

$$\text{FORMAT: } P_L = a f^c B^d$$

P_L in mW/cm^3 , B in kG, f in kHz





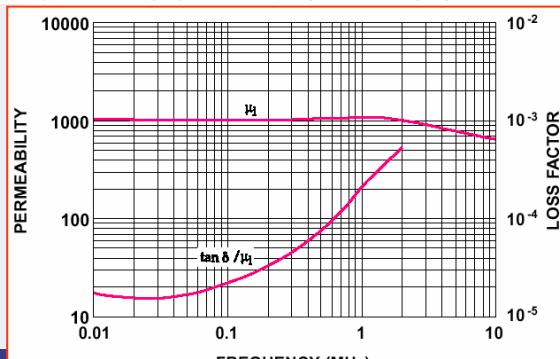
Core Losses Calculation

CORE LOSS vs PEAK AC FLUX DENSITY

$$\text{FORMULA: } CL(\text{mW/cm}^3) = \frac{f}{a + \frac{b}{B^{2.3}} + \frac{c}{B^{1.65}}} + (d f^2 B^2)$$



Material	a	b	c	d
-2	4.0×10^9	3.0×10^8	2.7×10^6	8.0×10^{-15}
-8	1.9×10^9	2.0×10^8	9.0×10^5	2.5×10^{-14}
-14	4.0×10^9	3.0×10^8	2.7×10^6	1.6×10^{-14}
-18	8.0×10^8	1.7×10^8	9.0×10^5	3.1×10^{-14}
-26	1.0×10^9	1.1×10^8	1.9×10^6	1.9×10^{-13}



Steward

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Winding Losses Calculation

1.

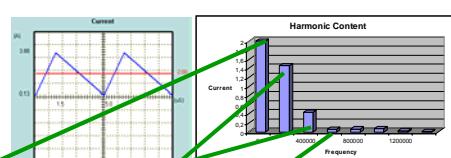
R_{DC}

$$P = I^2_{rms} * R_{DC}$$

$$R_{DC} = \rho \cdot \frac{\text{length}}{\text{Area}}$$

2.

R_{AC}



$$P = I^2_{DC} * R_{DC} + I^2_{rms_1} * R_{AC_1} + I^2_{rms_2} * R_{AC_2} + I^2_{rms_3} * R_{AC_3} + \dots$$

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Winding Losses Calculation

$$P = I_{DC}^2 * R_{DC} + I_{rms_1}^2 * R_{AC_1} + \\ + I_{rms_2}^2 * R_{AC_2} + I_{rms_3}^2 * R_{AC_3} + \dots$$

1.

Only Skin

$$\delta = \frac{1}{\sqrt{\pi f \mu_0 \sigma}}$$

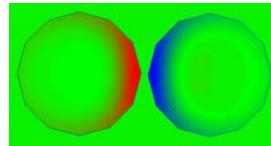
2.

Analytical (i.e. Dowell)

$$K_r = \frac{R_{AC}}{R_{DC}} = 0.5y \left[M(y) + (2m-1)^2 \cdot D(y) \right]$$

3.

FEA



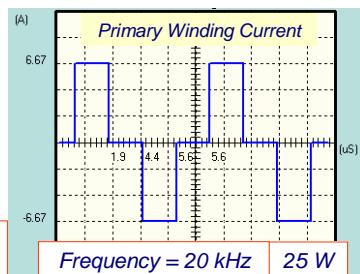
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Winding Losses Calculation. Example 1.

RM7/1
AWG 26
(2 skin depths)
 $n_1=n_2=12$ (2 parallel)



$$P = I_{rms}^2 * R_{DC}$$

$$R_{DC} \rightarrow 1.506 W$$

$$P = I_{DC}^2 * R_{DC} + I_{rms_1}^2 * R_{AC_1} + \\ + I_{rms_2}^2 * R_{AC_2} + I_{rms_3}^2 * R_{AC_3} + \dots$$

Skin

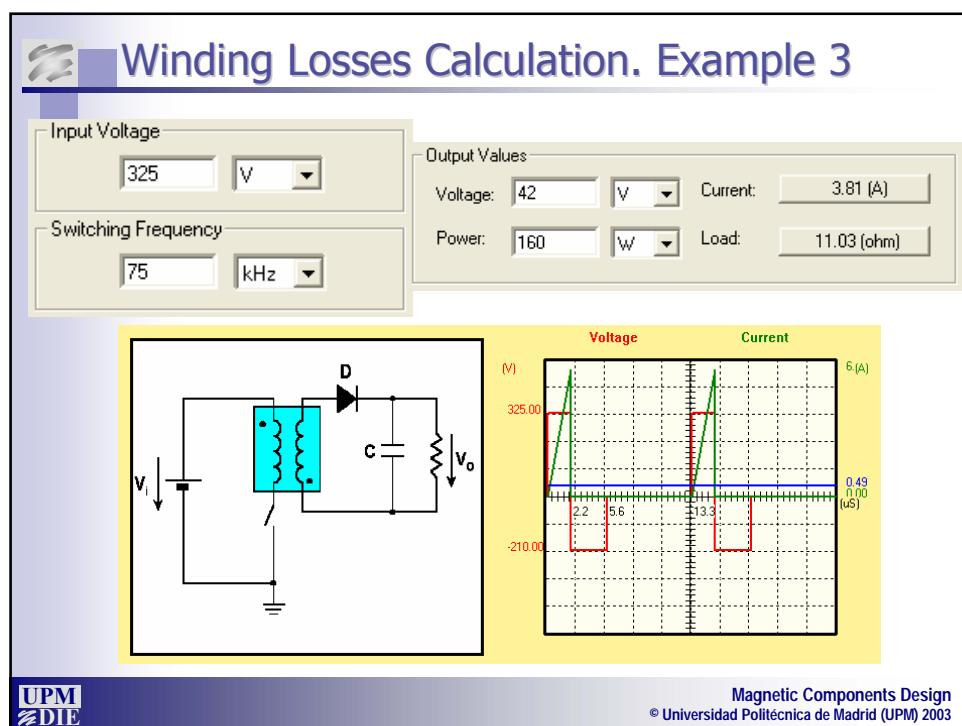
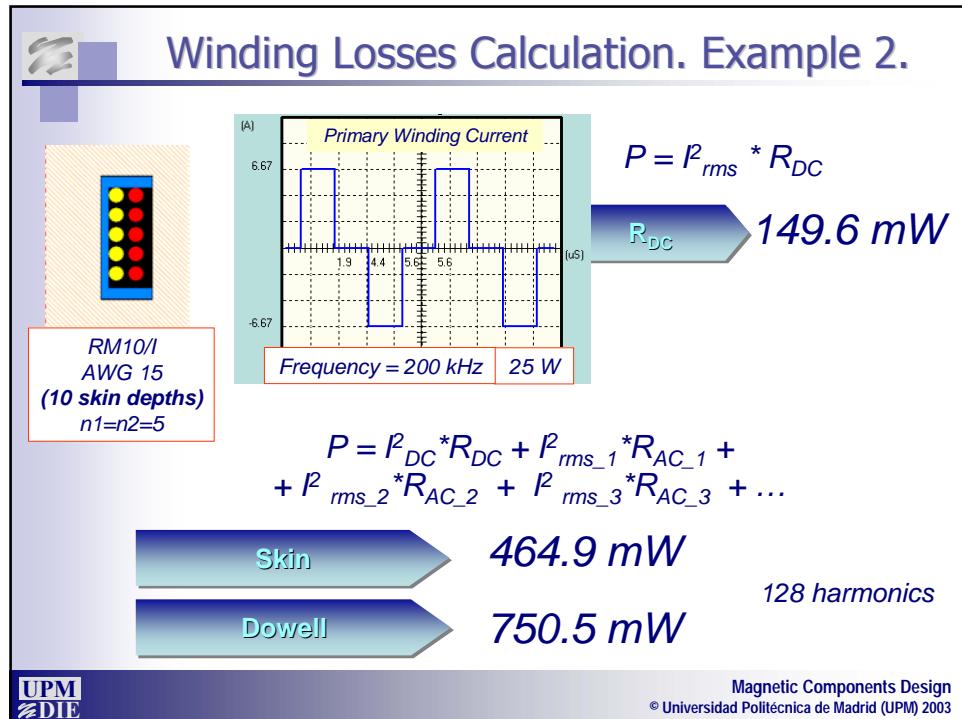
$$1.529 W$$

128 harmonics

Dowell

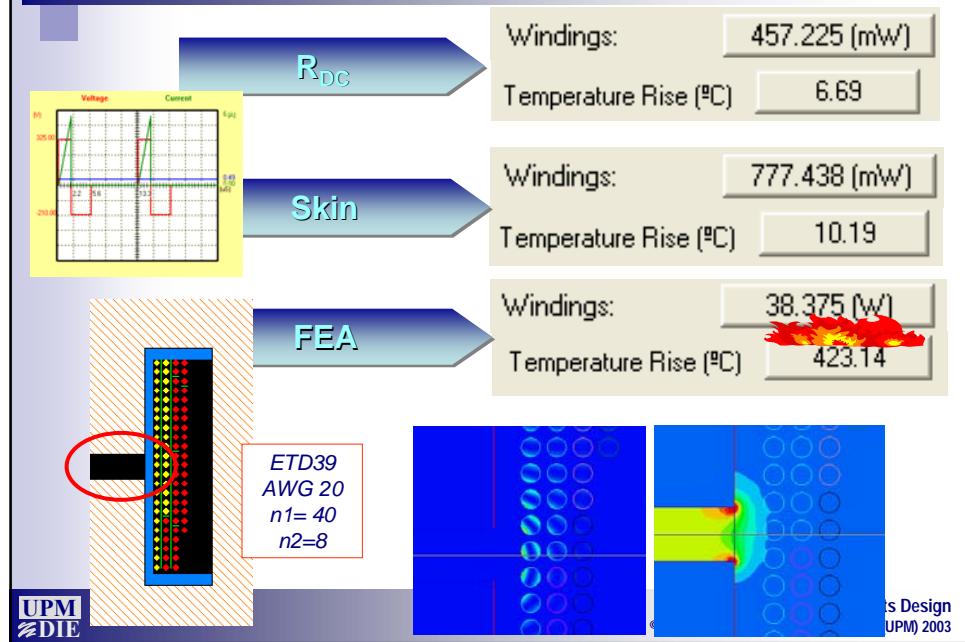
$$1.527 W$$

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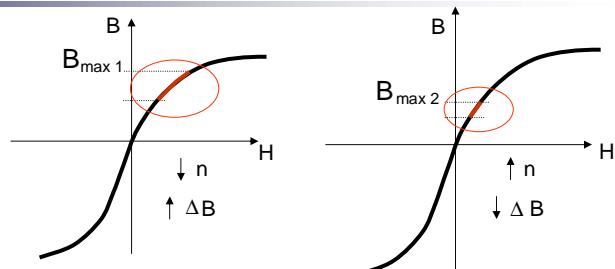
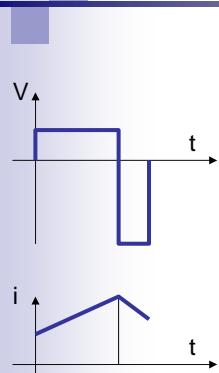




Winding Losses Calculation. Example 3



Optimization (I)



$$n \cdot \Delta B = \frac{V \cdot \Delta t}{\text{Area}} \Rightarrow n \cdot \Delta B = \text{Constant}$$

$$n \cdot B_{max} = \frac{L \cdot i_{max}}{\text{Area}} \Rightarrow n \cdot B_{max} = \text{Constant}$$

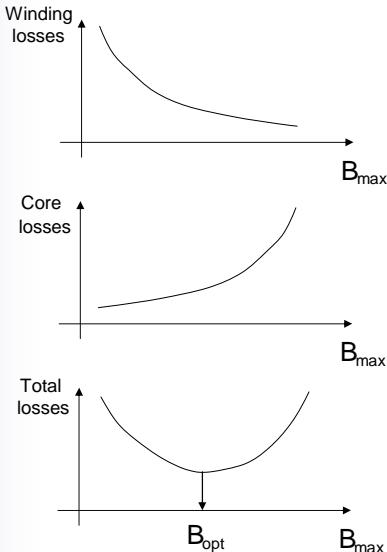
$\uparrow B_{max} \Rightarrow \left\{ \begin{array}{l} \downarrow n \\ \uparrow \Delta B \end{array} \right\} \Rightarrow \left\{ \begin{array}{l} \downarrow \text{Copper Losses} \\ \uparrow \text{Core Losses} \end{array} \right\}$



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Optimization (II)



$$\uparrow B_{max} \Rightarrow \downarrow n$$

$$P = I^2_{rms} \cdot n \cdot \rho \cdot \frac{\text{length}}{\text{Area}}$$

$$\uparrow B_{max} \Rightarrow \uparrow \Delta B$$

$$P = V_e \cdot k \cdot f^\alpha \cdot \left(\frac{\Delta B}{2} \right)^\beta$$

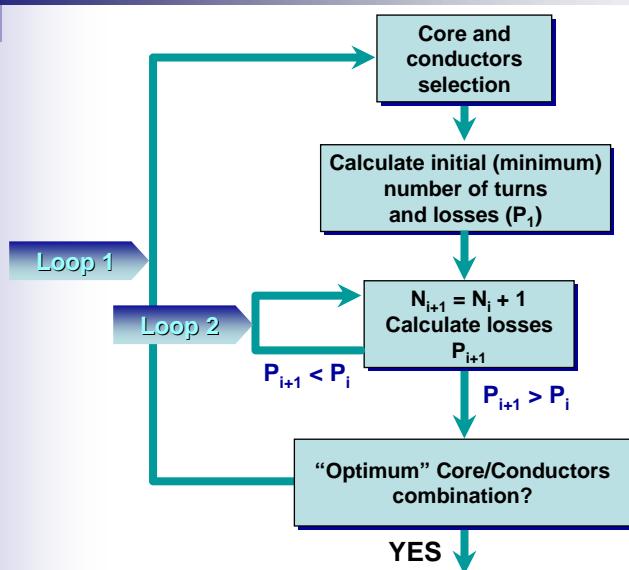


B_{opt} is below or above saturation?

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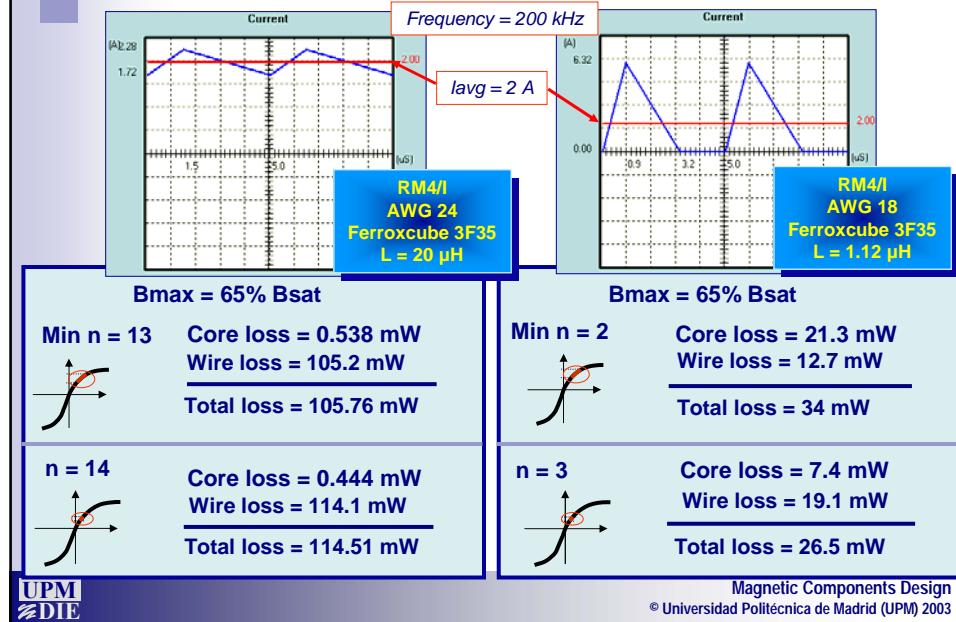
Optimization (III)



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Optimization Example. Inductor



Inductors

Calculation of the total reluctance

$$L = \frac{N^2}{\mathfrak{R}_T} = N^2 \cdot A_L \rightarrow \mathfrak{R}_T = \frac{N^2}{L}$$

$$A_L = \frac{1}{\mathfrak{R}_T}$$

■ \mathfrak{R}_T is the total reluctance of the magnetic circuit.

■ This reluctance may be obtained using:

- ✓ Ferrite core + air gap
- ✓ A material with distributed gap (low permeability) like iron powder

Inductors

Calculation of the air gap length

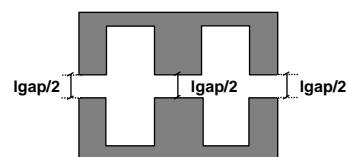
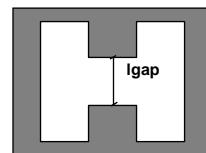
$$\mathfrak{R}_T = \mathfrak{R}_{ferrite} + \mathfrak{R}_{air} = \frac{1}{\mu_o \mu_e} \cdot \frac{l_e}{A_e} + \frac{1}{\mu_o} \cdot \frac{l_{gap}}{A_e}$$

$1/A_L$
(ferrite without gap)

$$\mathfrak{R}_T = \frac{1}{A_L} + \frac{1}{\mu_o} \cdot \frac{l_{gap}}{A_e}$$

$$\frac{1}{A_{L_T}} = \frac{1}{A_L} + \frac{l_{gap}}{\mu_o \times A_e}$$

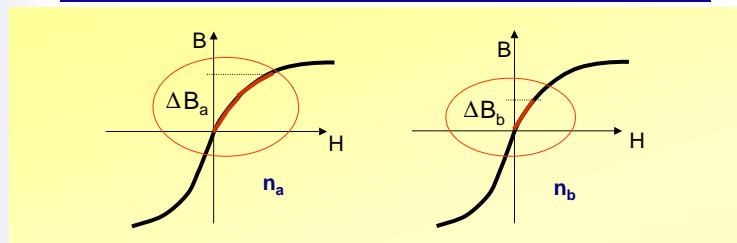
$$l_{gap} = \mu_o A_e \left[\frac{1}{A_{L_T}} - \frac{1}{A_L} \right]$$



Transformers

Number of turns

Number of turns calculated to keep maximum flux density or core losses under an appropriate value

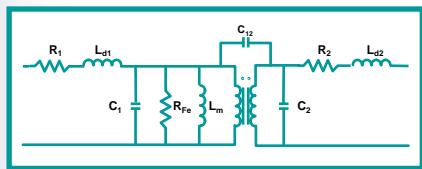


$$V_1 = N_1 \cdot \frac{\Delta \Phi}{\Delta t} = N_1 \cdot A_e \cdot \frac{\Delta B}{\Delta t} \rightarrow$$

$$N_1 = \frac{V_1 \Delta t}{A_e \Delta B}$$

$$a = \frac{N_1}{N_2} \Rightarrow N_2 = \frac{N_1}{a}$$

Modeling



$$\frac{\partial E(z,t)}{\partial z} = \mu \frac{\partial H(z,t)}{\partial t}$$

$$\frac{\partial H(z,t)}{\partial z} = \sigma \cdot E(z,t) + \epsilon \frac{\partial E(z,t)}{\partial t}$$

Modeling for Virtual Prototyping?

Do I make simulations?

Do I trust them?

if not, are magnetic component models the reason?

Model

...tool to obtain
MY OWN
design guidelines

...gate to
simulation



Modeling steps

Physical description (equations)

Equivalent Electrical model

Parameters extraction

Model solving



Physics

Physical description (equations)

Maxwell equations

$$\nabla \cdot \mathbf{D} = \chi$$

$$\nabla_x \mathbf{E} = -\mu \frac{\partial \mathbf{H}}{\partial t}$$

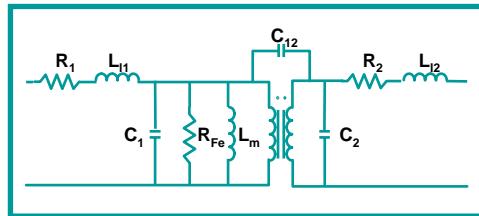
$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla_x \mathbf{H} = \sigma \mathbf{E} + \epsilon \frac{\partial \mathbf{E}}{\partial t}$$

Equivalent Circuit (I)

Equivalent Electrical model

Discrete elements



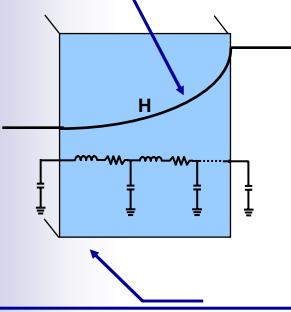
Frequency Independent (only for sinusoidal waveforms)

Equivalent Circuit (II)

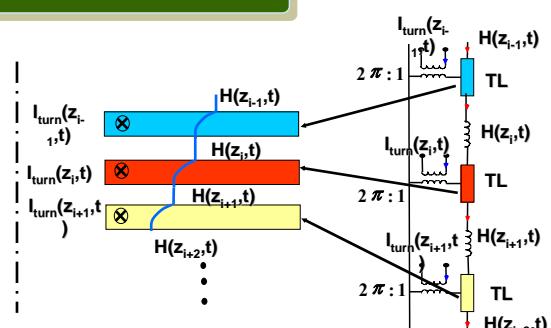
Equivalent Electrical model

Transmission lines based

1D Maxwell equations



Transmission line equations

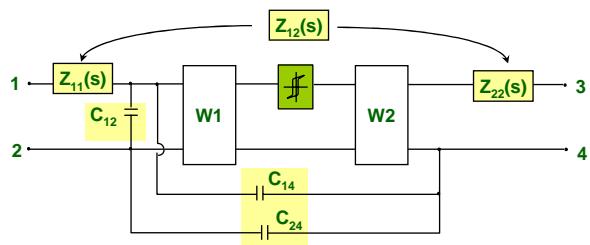


Frequency dependent
Magnetic/Electric Analogy based

Equivalent Circuit (III)

Equivalent Electrical model

Behavioral



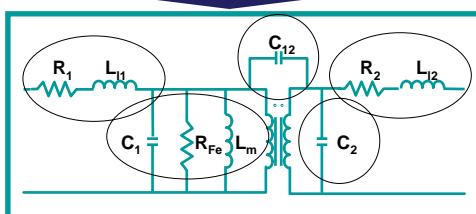
Frequency dependent
More Flexible behavior

UPM
DIE

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Parameters Extraction (I)

Parameters extraction

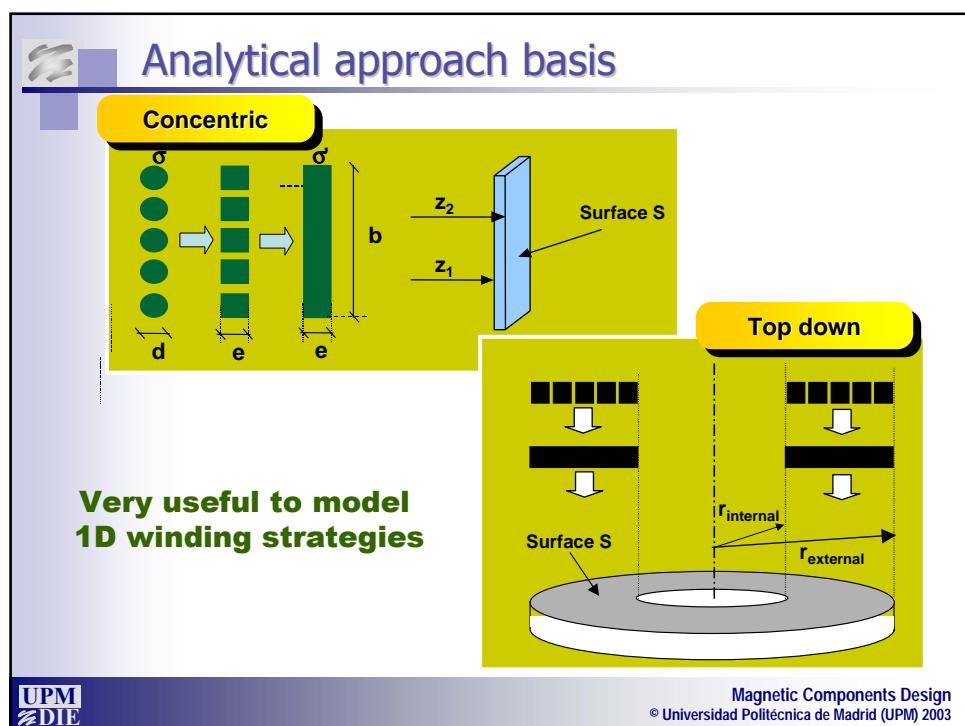
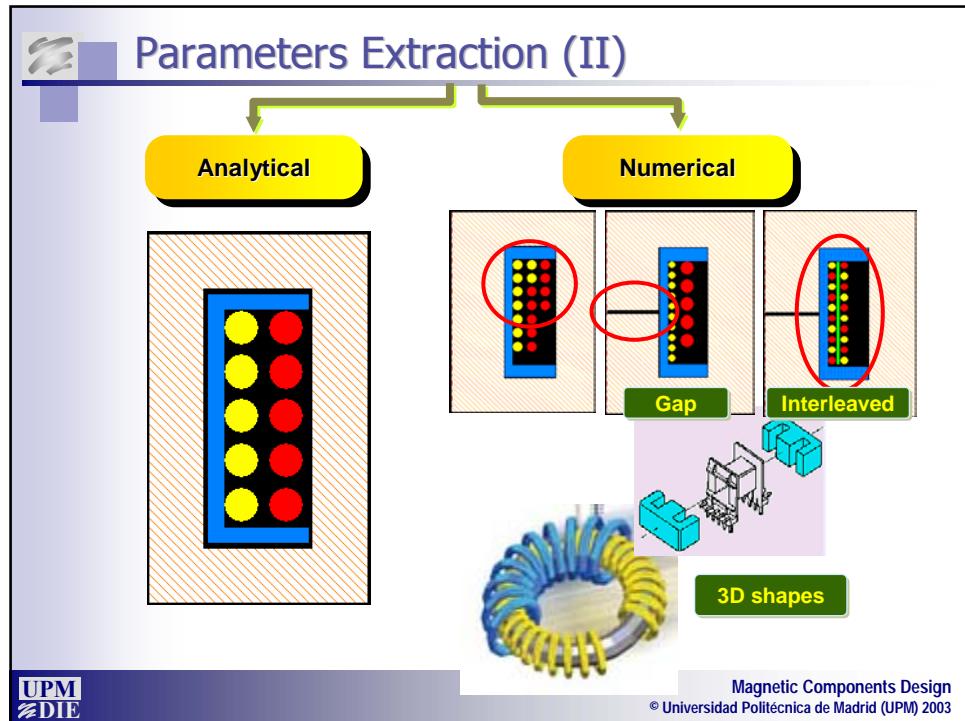


Analytical

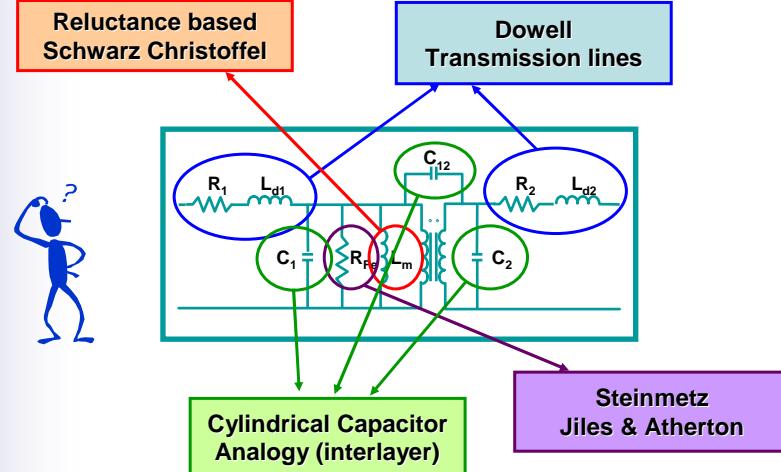
Numerical

UPM
DIE

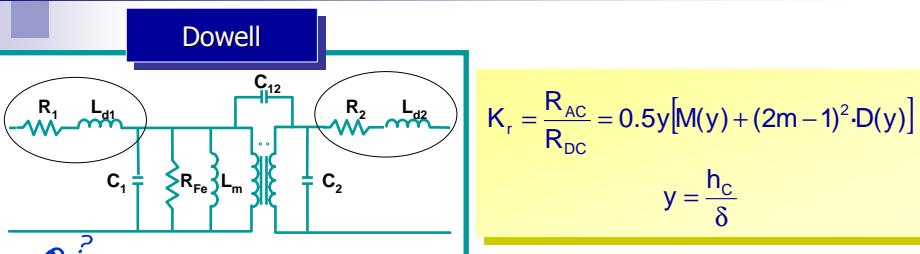
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Analytical approach possibilities



Analytical approach examples (I)



$$K_r = \frac{R_{AC}}{R_{DC}} = 0.5y [M(y) + (2m-1)^2 \cdot D(y)]$$

$$y = \frac{h_c}{\delta}$$

h_c = Layer thickness
 δ = Skin depth
 m = Number of layers of the winding sector

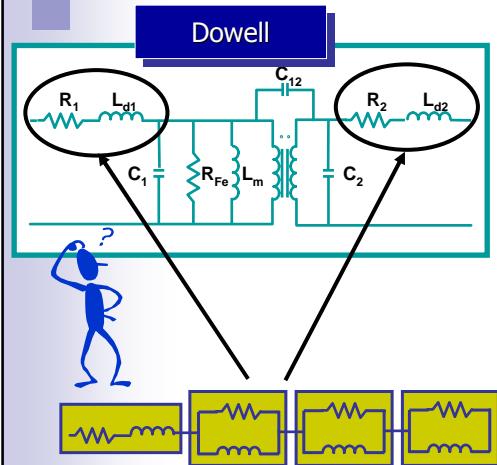
$$M(y) = \frac{\sinh(y) + \sin(y)}{\cosh(y) - \cos(y)}$$

$$D(y) = \frac{\sinh(y) - \sin(y)}{\cosh(y) + \cos(y)}$$

Calculation valid for a single frequency (sinusoidal)



Analytical approach examples (II)



Analytical approach examples (III)

Transmission line based parameters extraction

1D Maxwell equations

$$\frac{\partial E(z,t)}{\partial z} = \mu \frac{\partial H(z,t)}{\partial t}$$

$$\frac{\partial H(z,t)}{\partial z} = \sigma \cdot E(z,t) + \epsilon \frac{\partial E(z,t)}{\partial t}$$

Transmission line equations

$$\frac{\partial V(z,t)}{\partial z} = \cancel{X} \cdot I(z,t) + L \frac{\partial I(z,t)}{\partial t}$$

$$\frac{\partial I(z,t)}{\partial z} = G \cdot V(z,t) + C \frac{\partial V(z,t)}{\partial t}$$

$$C = \epsilon \cdot S$$

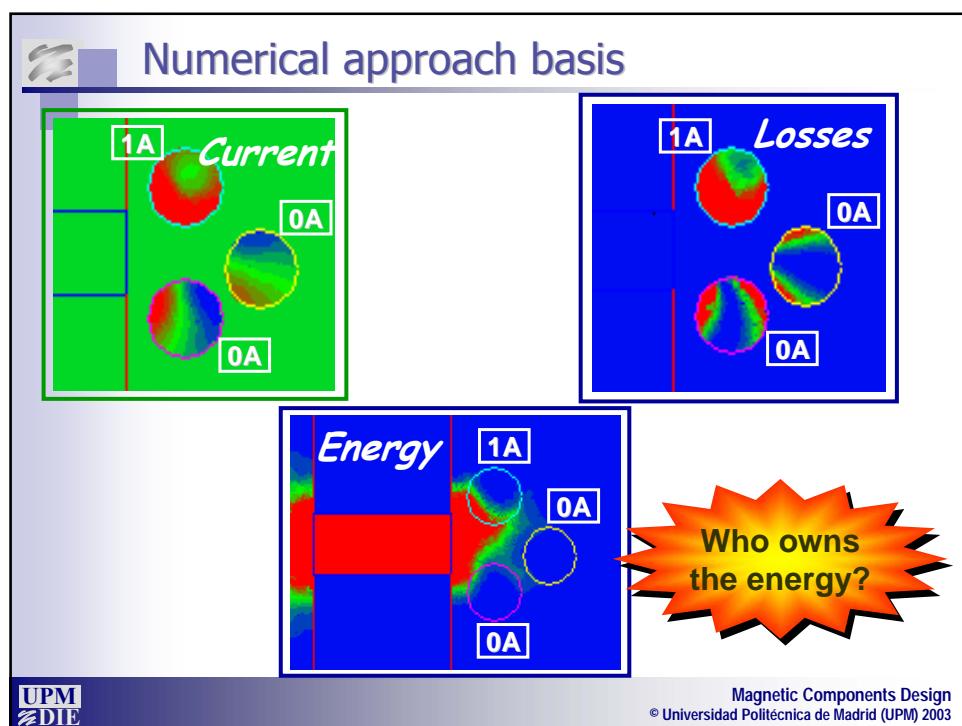
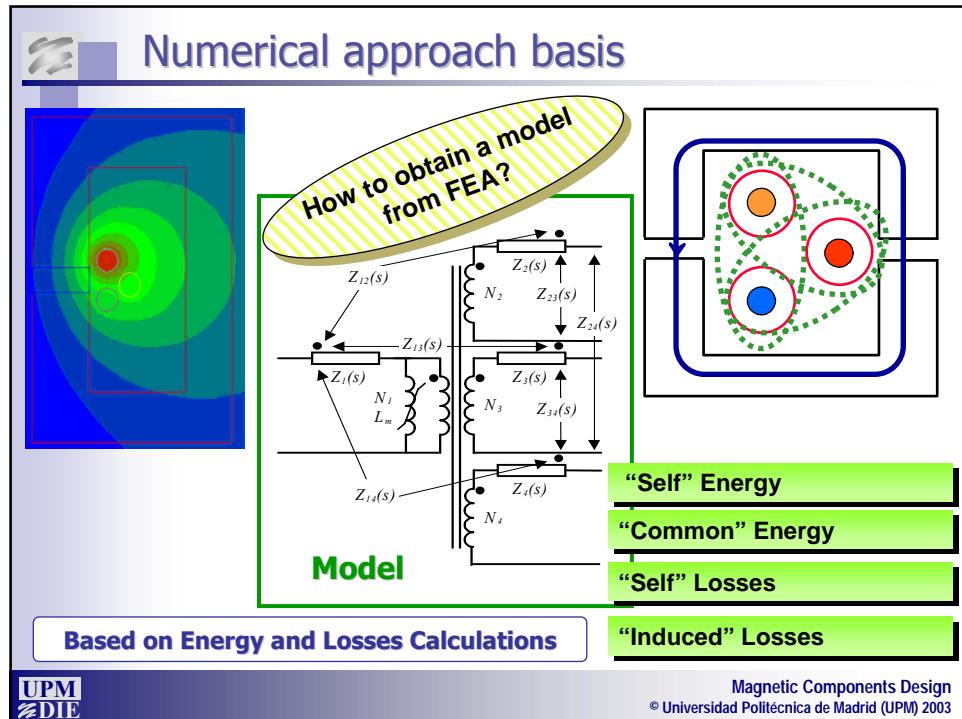
Electric energy

G = $\sigma \cdot S$

Losses

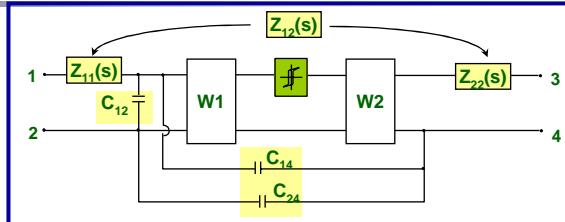
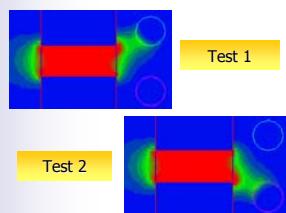
$$L = \frac{\mu}{S}$$

Magnetic energy





Numerical approach example



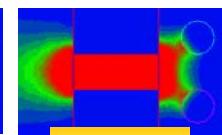
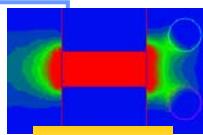
Z_{11}, Z_{22} :

✓ Energy and losses due to I_1 OR I_2 INDEPENDENTLY

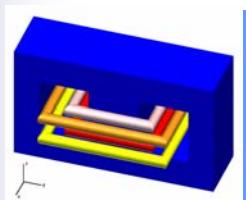
$$Z(s) = c_0 + c_1 s + \sum_{i=1}^{NPF} \frac{c_{2i}s}{s + c_{2i-1}}$$

Z_{12} : **Coupling?**

✓ Energy and losses due to I_1 AND I_2 SIMULTANEOUSLY



Numerical approach application (I)



**Energy and losses
should be the same**

Energy in the core

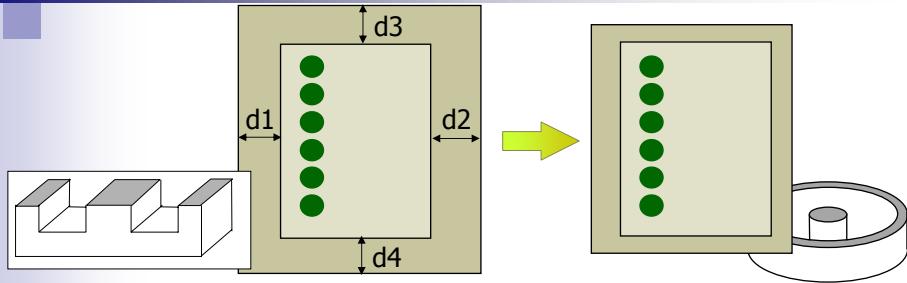
Energy in the window

Energy in the air gap

Losses in the core

Losses in the conductors

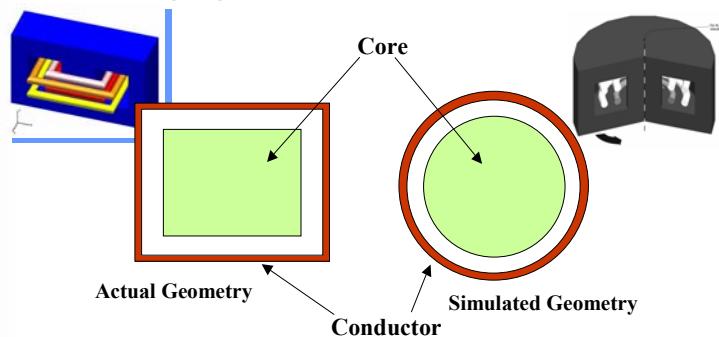
Numerical approach application (II)



- Window Height and Window Width are the same in both structures
- d1 is modified in order to obtain the same central leg area in both structures
- d2 is modified in order to obtain the same external leg area in both structures
- d3 is modified in order to obtain the same core volume in both structures

Numerical approach application (III)

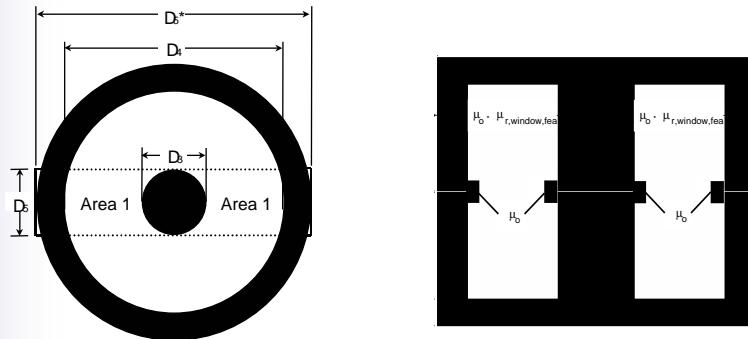
Modification of properties: Conductors Resistance



$$R_{model} = \frac{length_{actual}}{length_{model}} R_{actual}$$

Numerical approach application (IV)

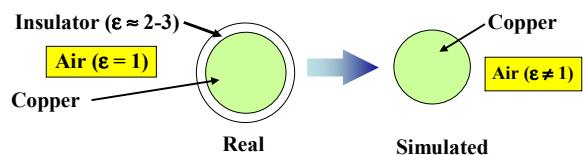
Modification of properties: Window Air Permeability



$$\mu_{r,window,fea} \cdot \mu_0 = \frac{Area~1}{Area~2} \cdot \mu_0$$

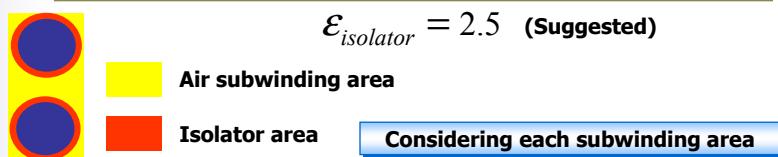
Numerical approach application (V)

Modification of properties: Window Air Permittivity

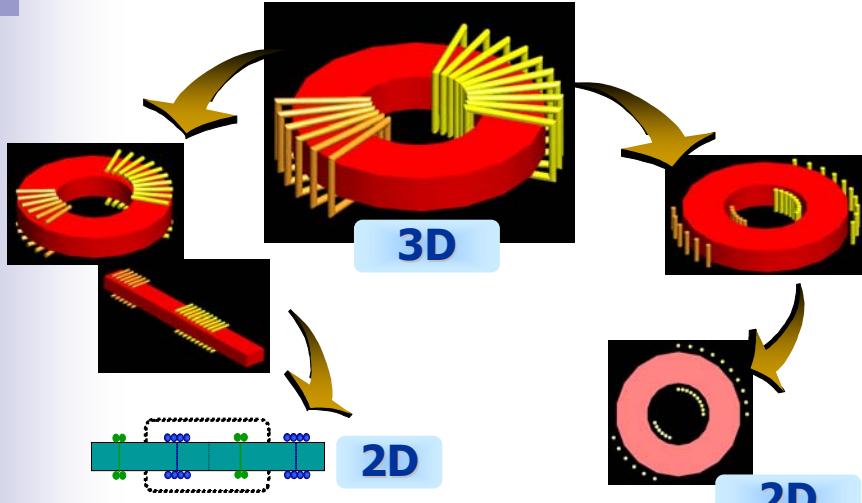


$$\epsilon_{model} = \frac{\epsilon_{isolator} \cdot Area_{wire isolator} + \epsilon_{air} \cdot Area_{air}}{Area_{wire isolator} + Area_{air}}$$

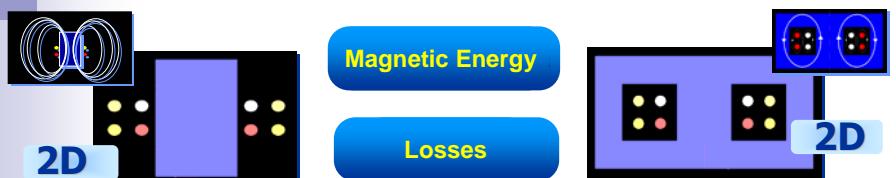
$$\epsilon_{isolator} = 2.5 \text{ (Suggested)}$$



Double 2D concept: Application to Toroids

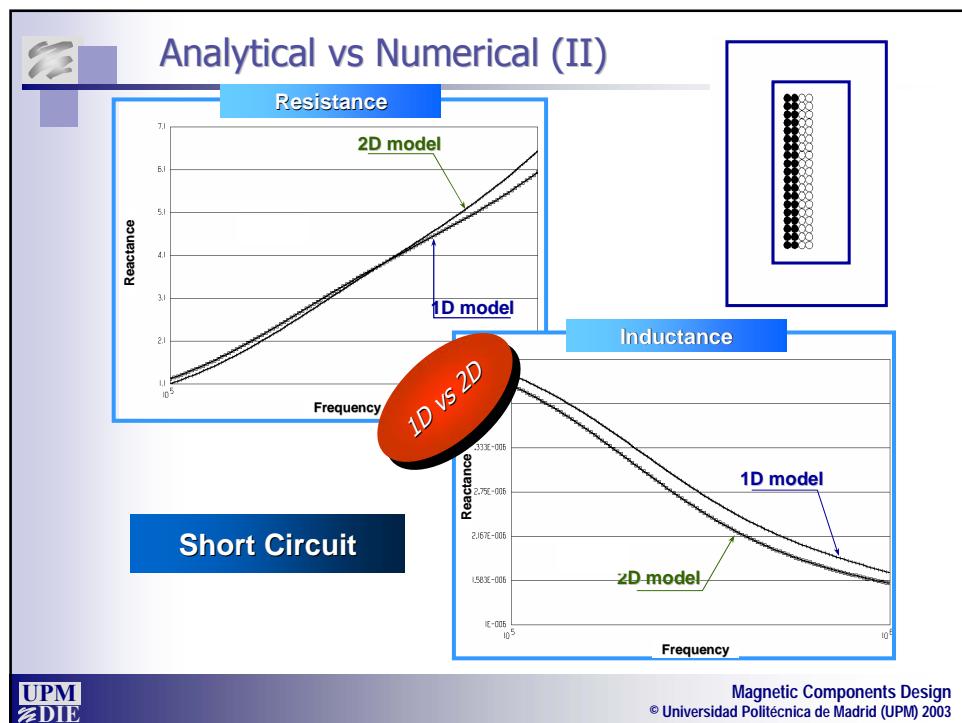
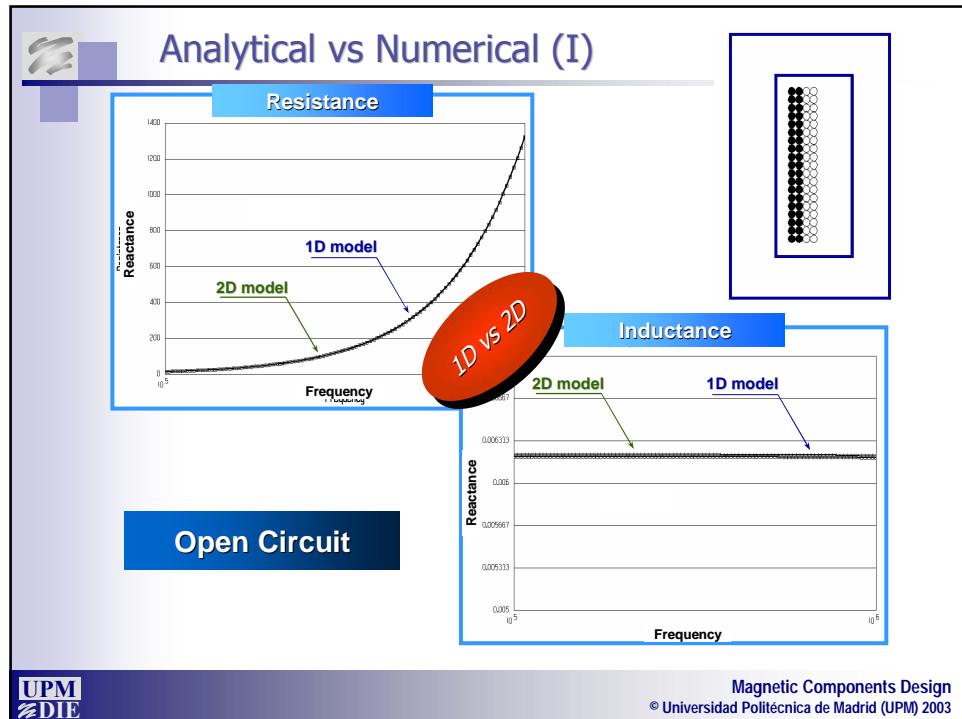


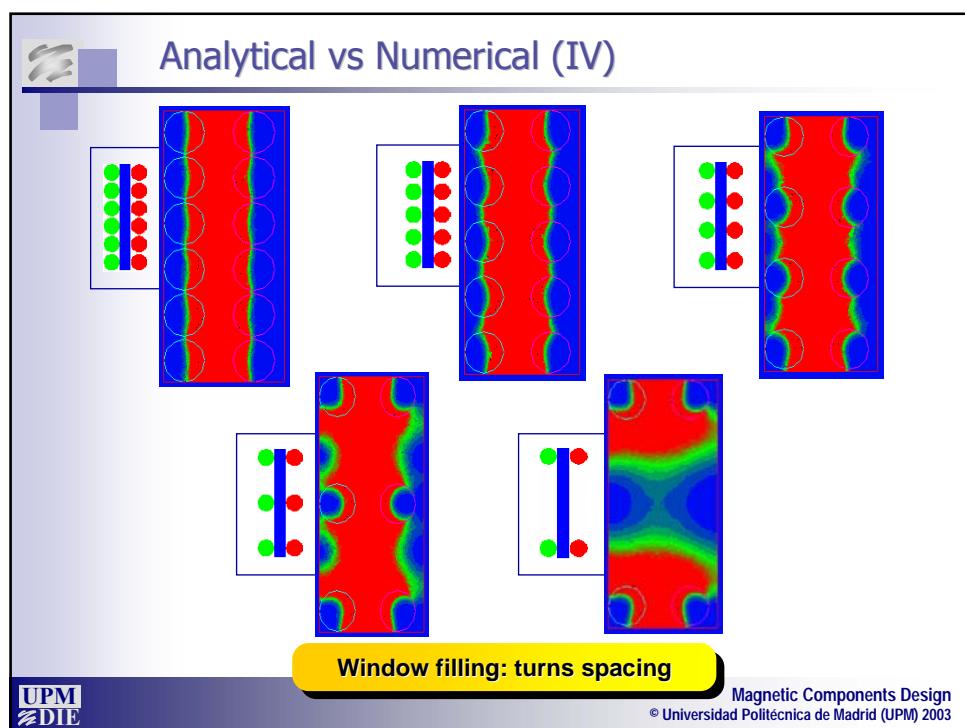
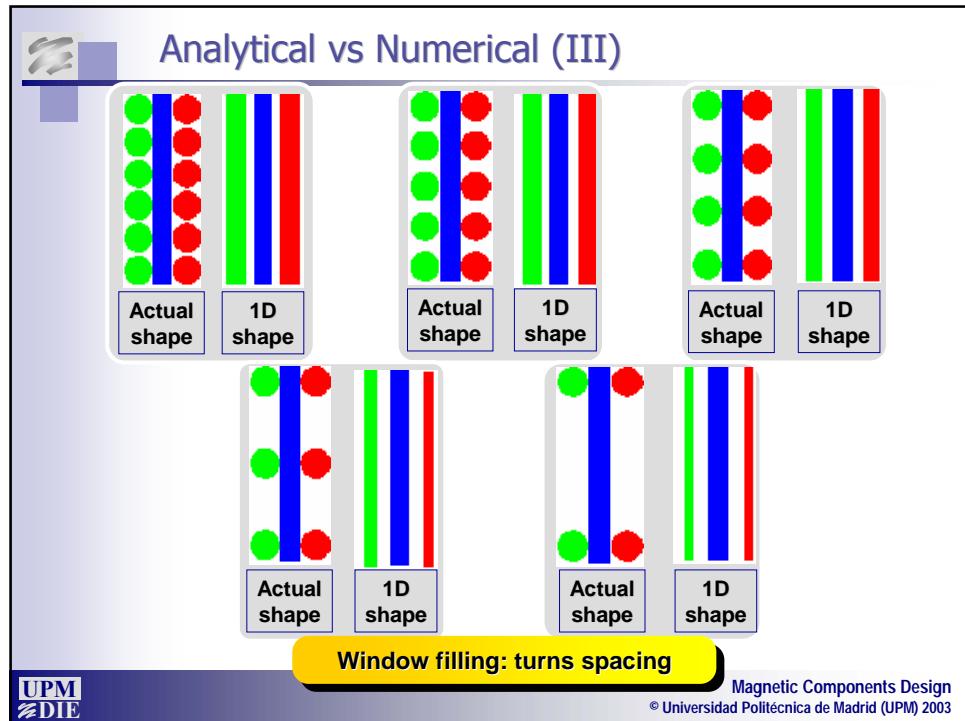
Double 2D concept

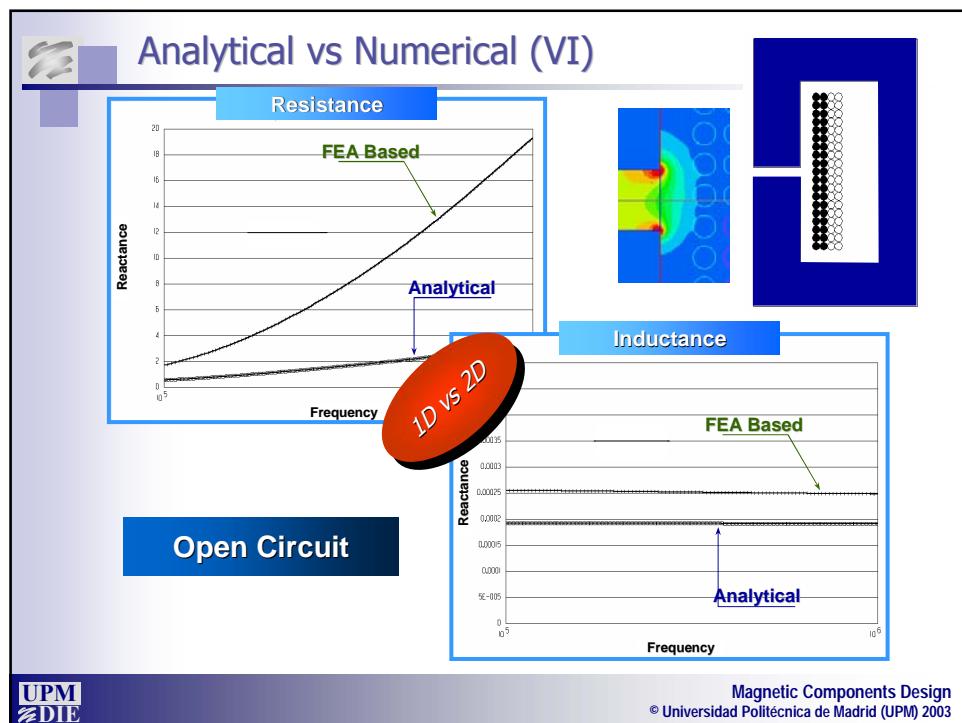
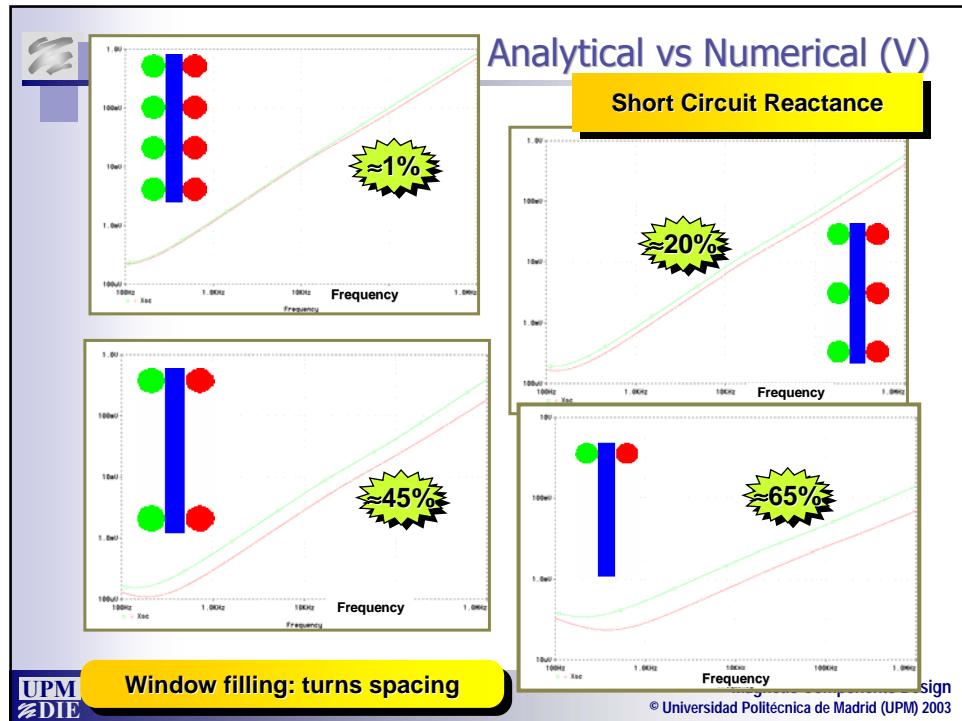


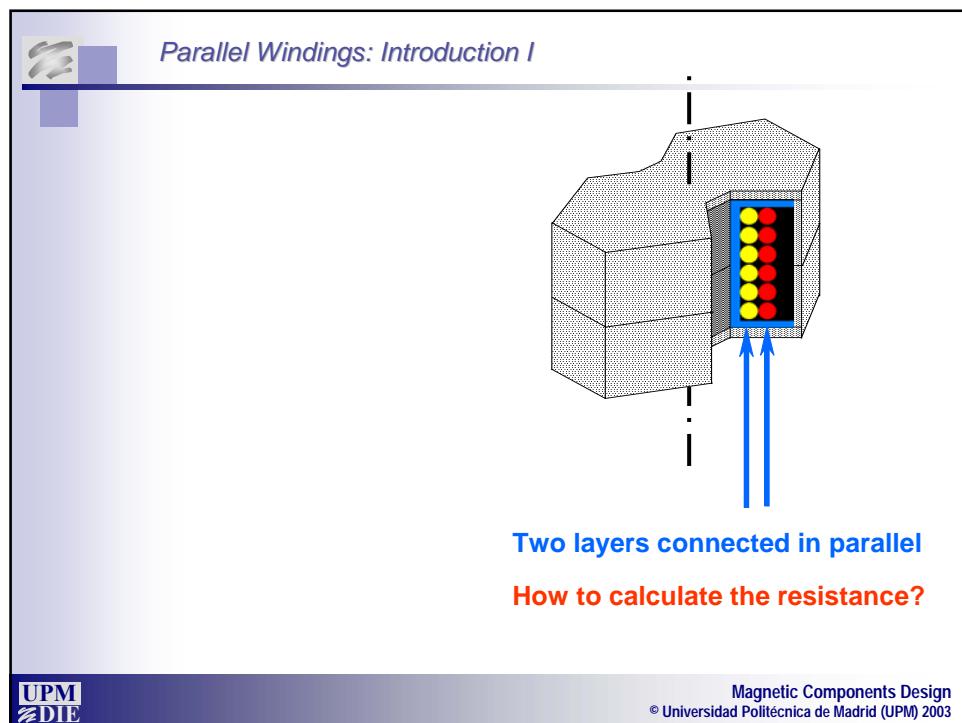
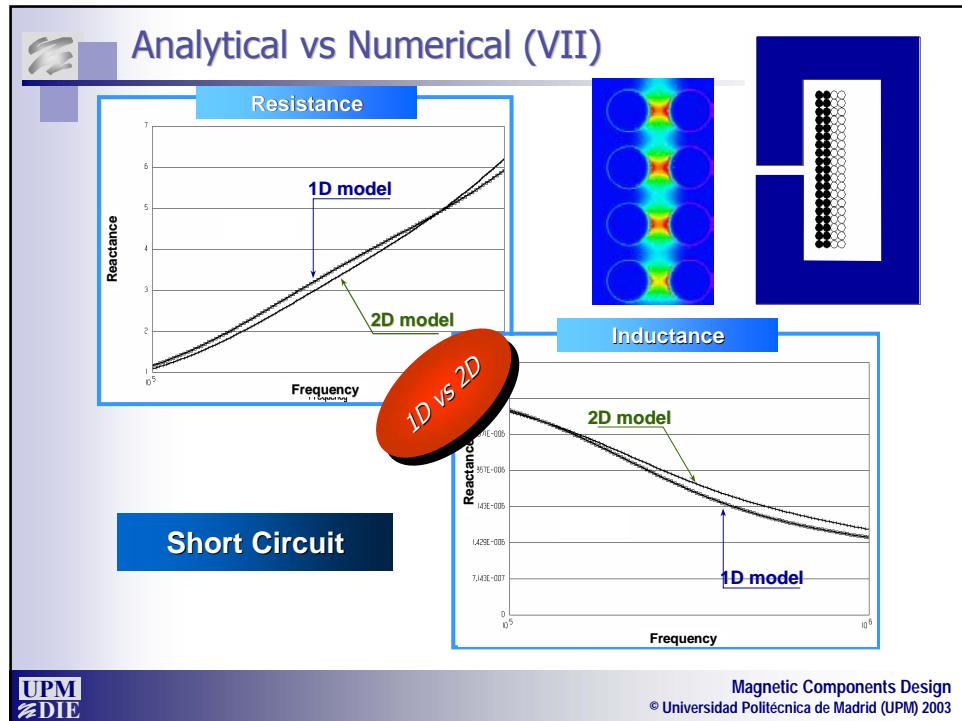
$$E_m = \frac{1}{2} \left[C_S \int B_S \cdot H_S^* dS + C_D \int B_D \cdot H_D^* dS \right]$$

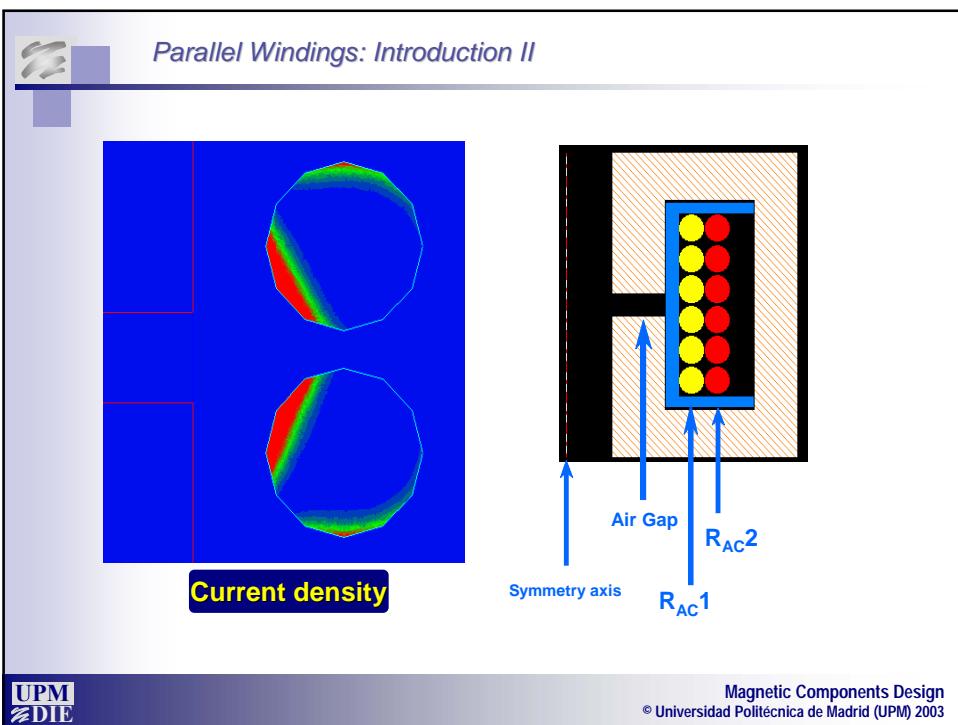
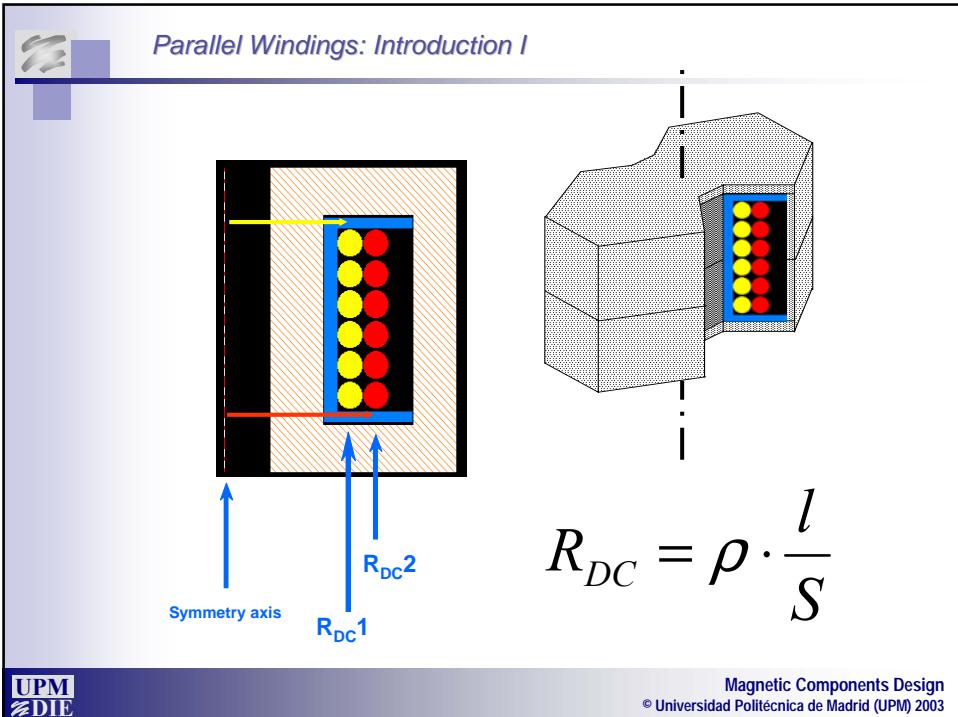
$$P_d = C_S \int \frac{J_S \cdot J_S^*}{\sigma} dS + C_D \int \frac{J_D \cdot J_D^*}{\sigma} dS$$



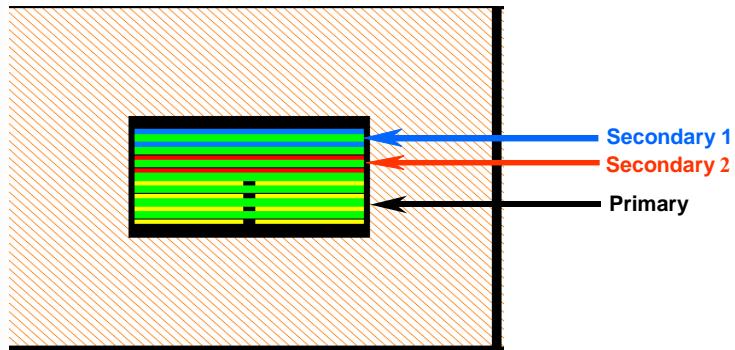






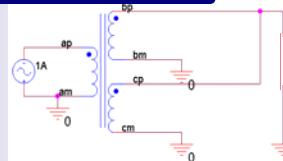


Parallel Windings: Introduction III

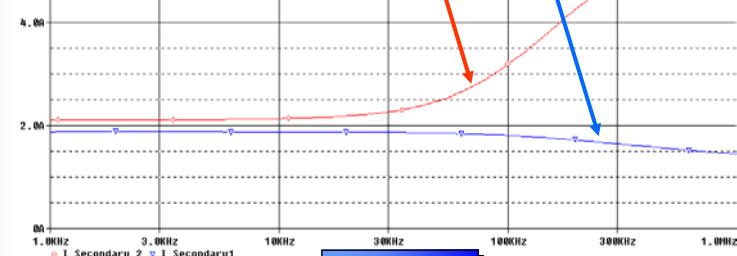


Parallel Windings: Introduction IV

Short Circuit Test



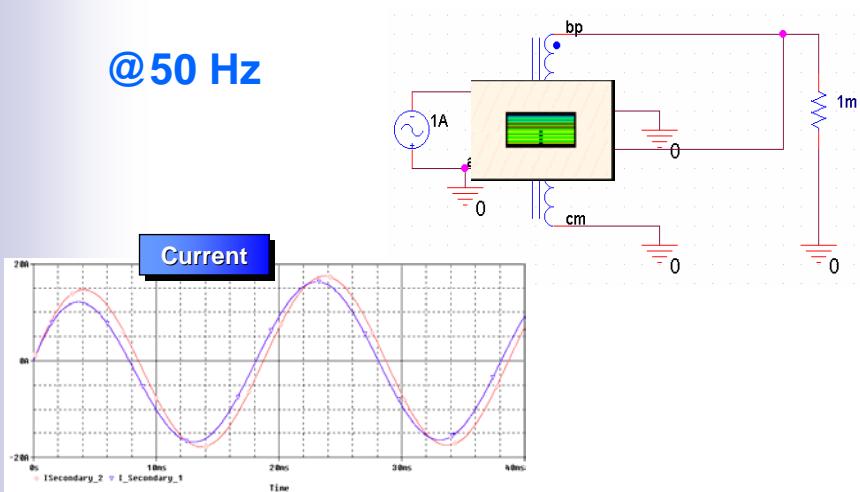
Current



Frequency

Parallel Windings: Introduction V

@ 50 Hz

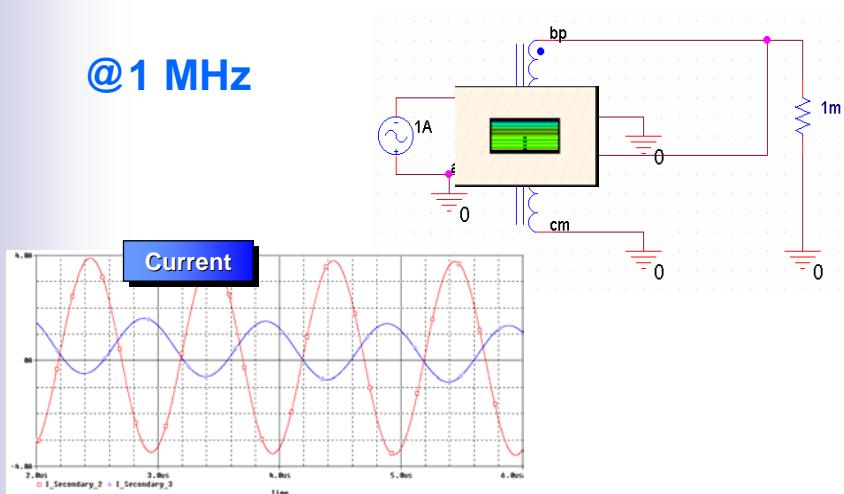


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Parallel Windings: Introduction VI

@ 1 MHz

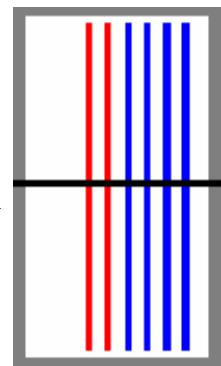
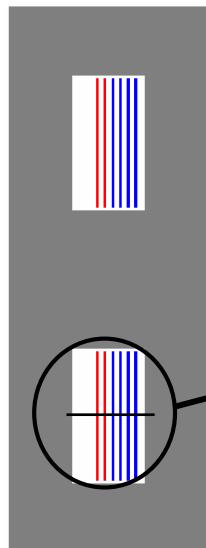
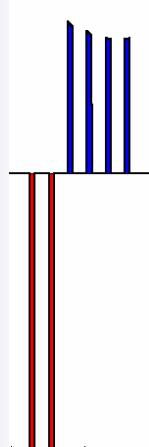


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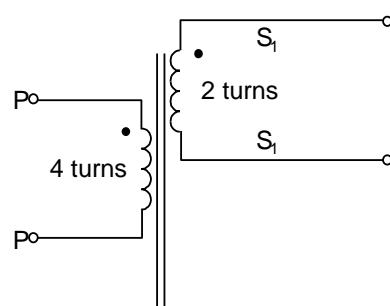
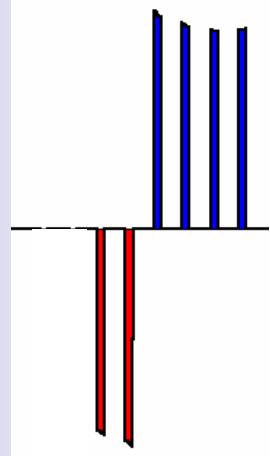


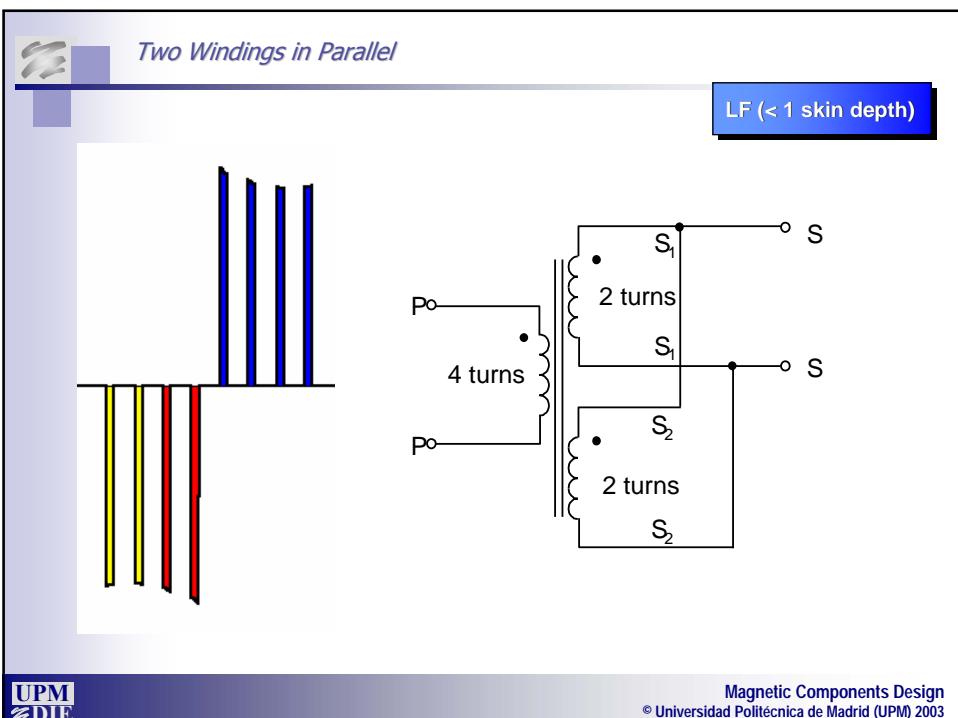
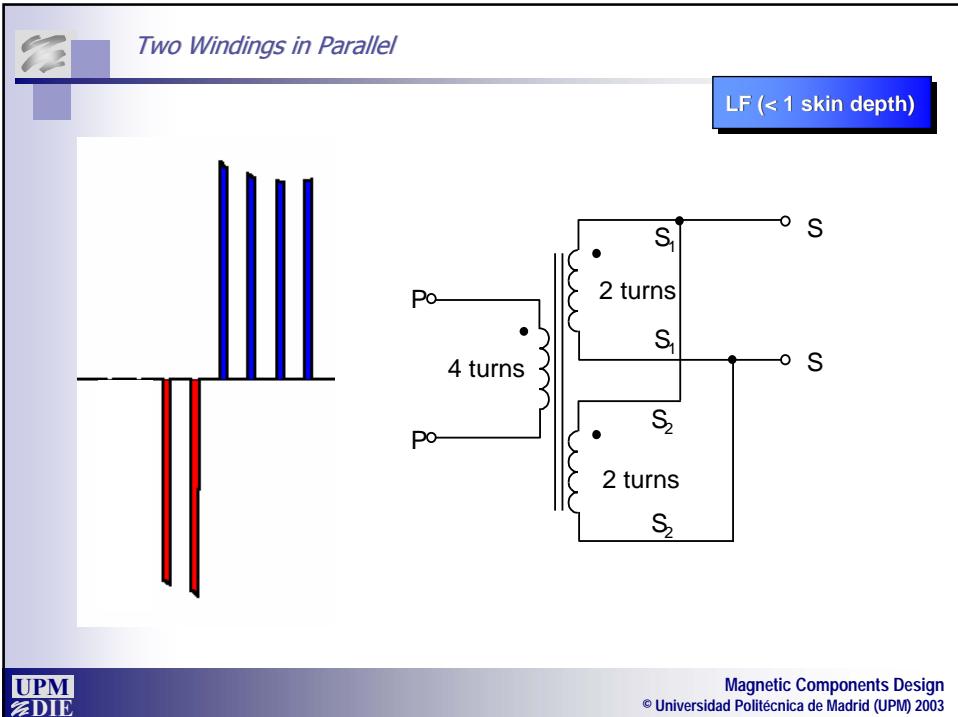
Analysis of different Winding Strategies

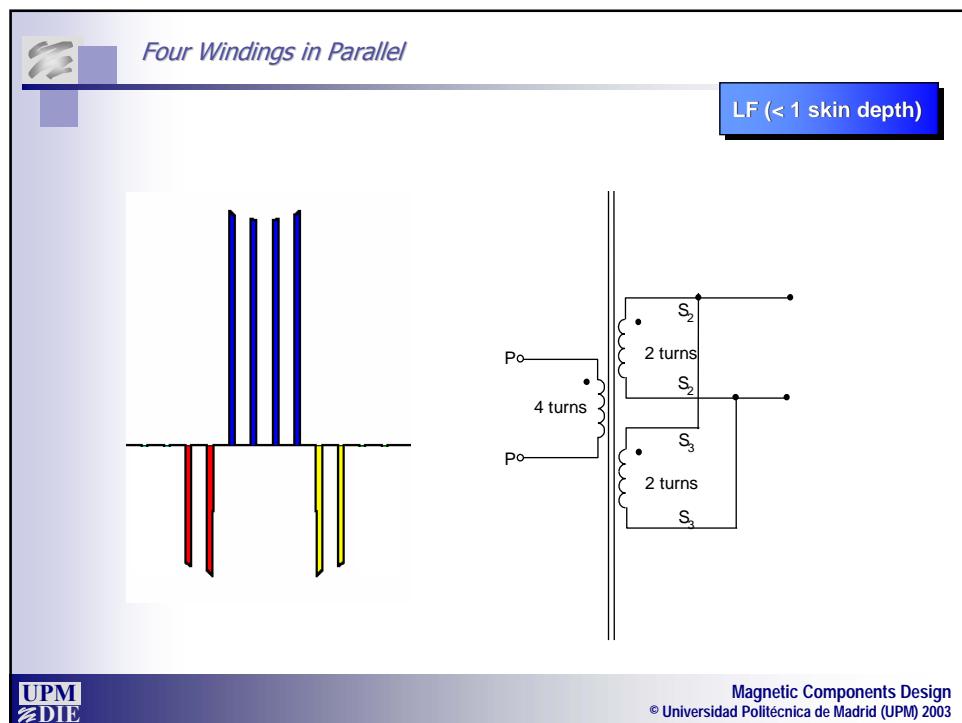
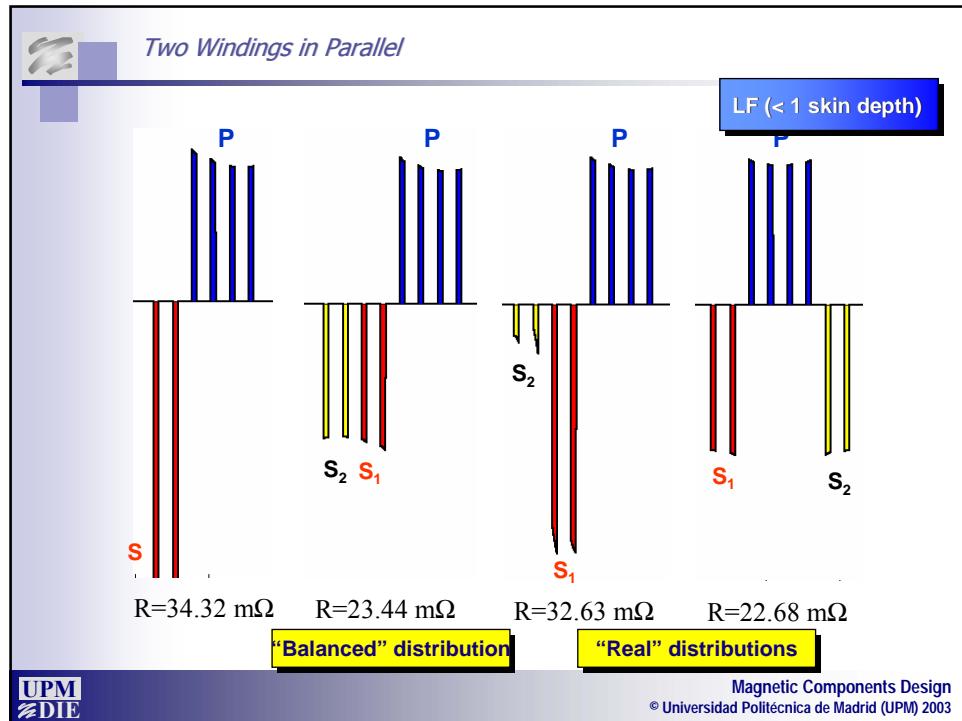


Two Windings in Parallel

LF (< 1 skin depth)



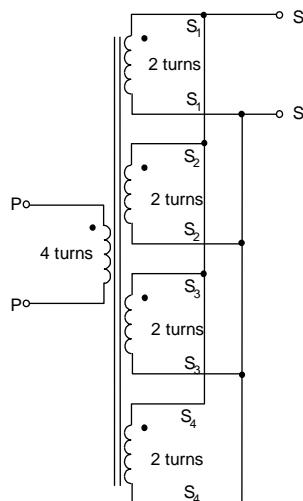
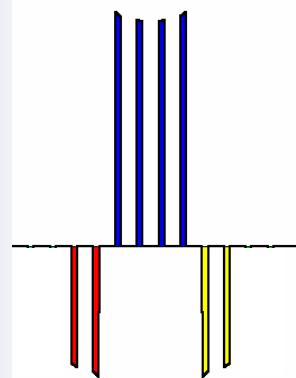






Four Windings in Parallel

LF (< 1 skin depth)

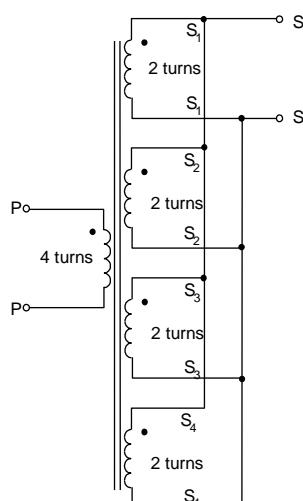
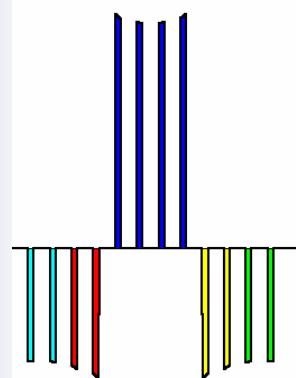


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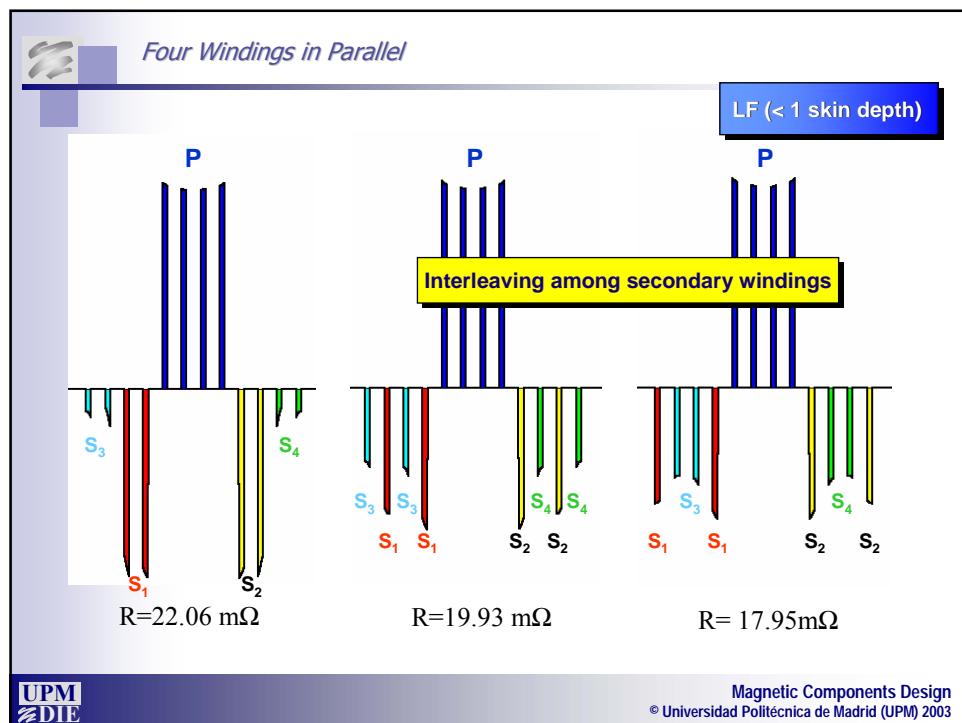
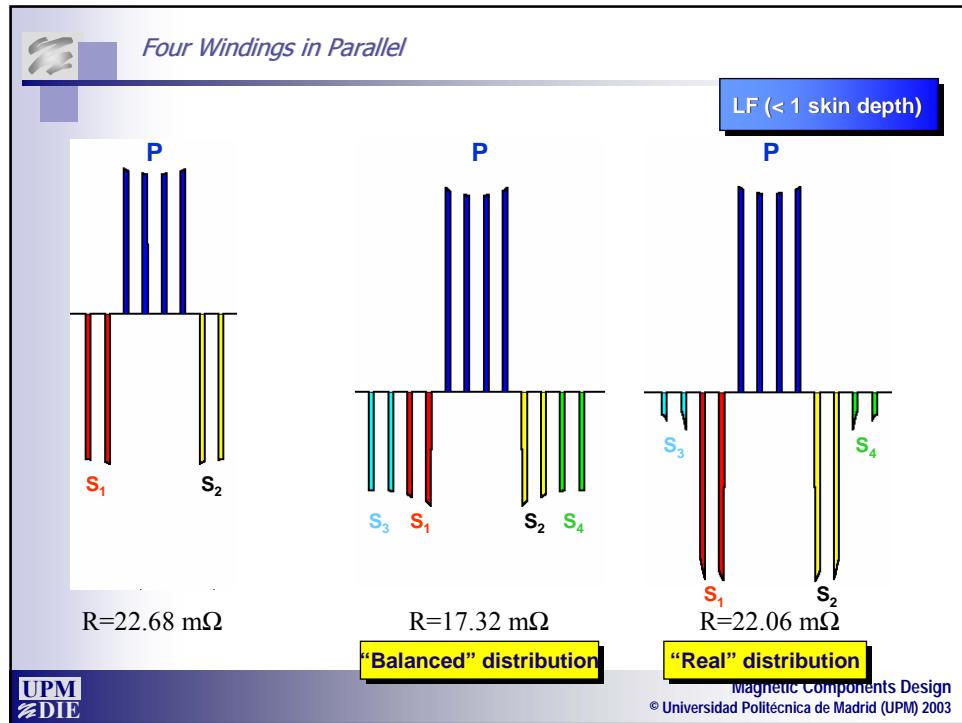


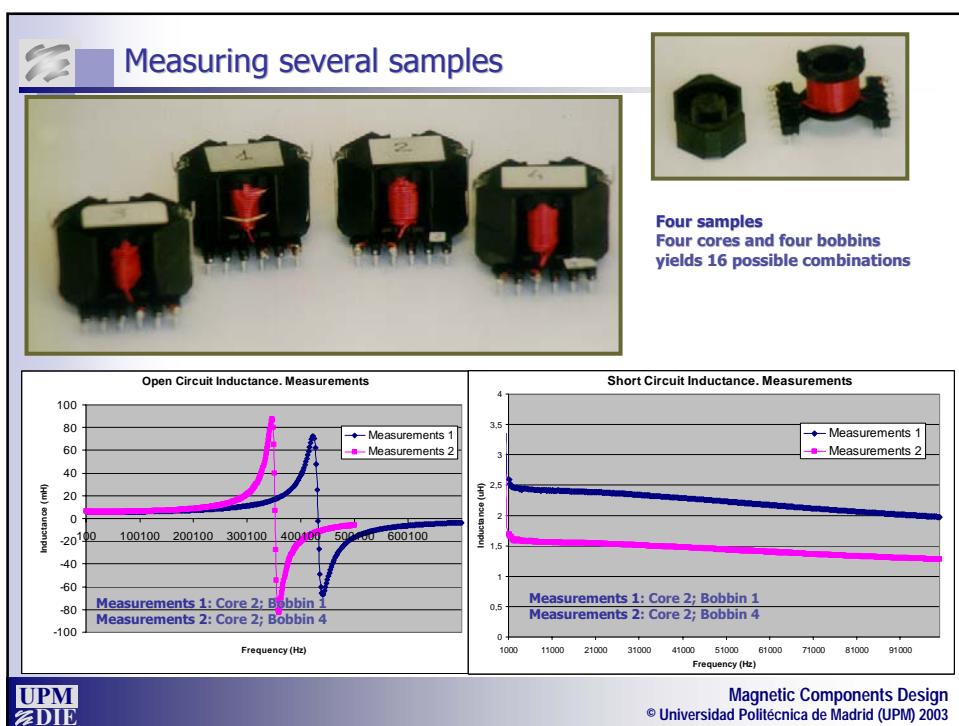
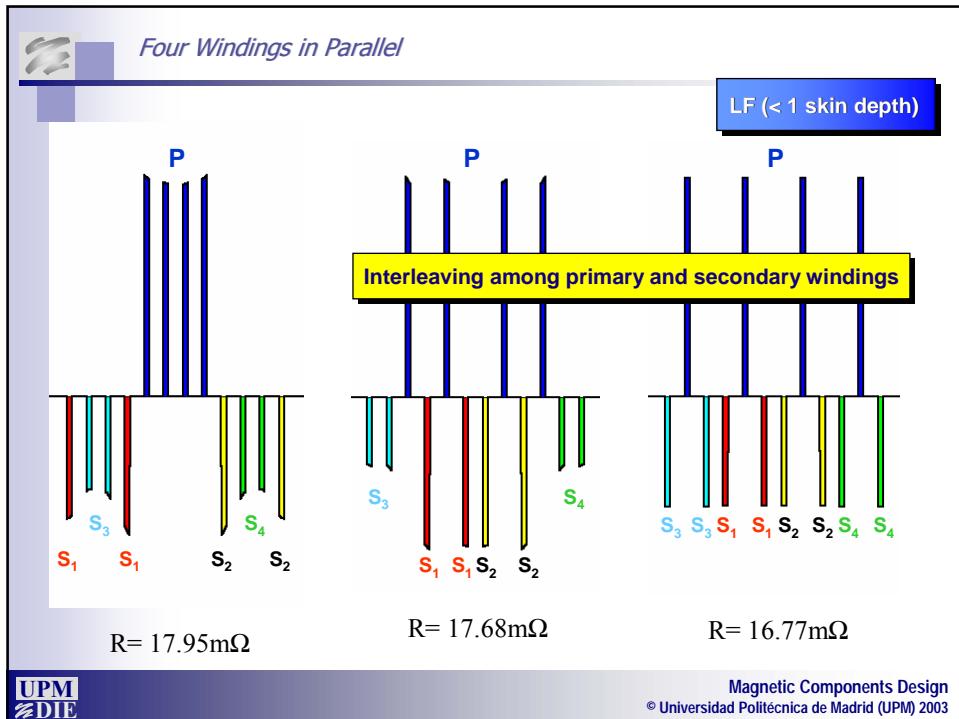
Four Windings in Parallel

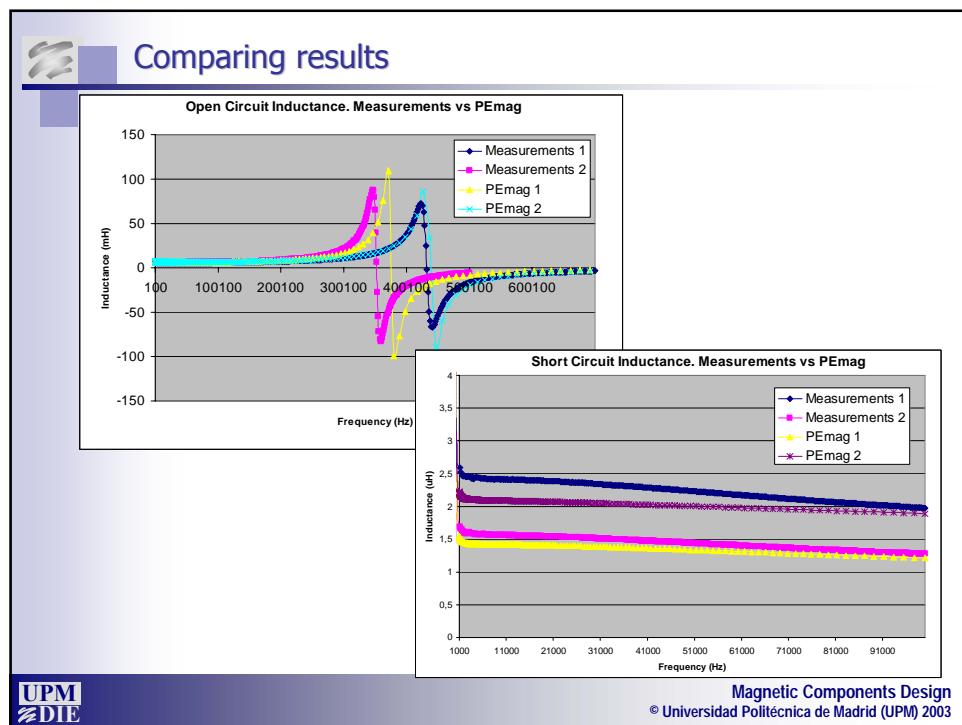
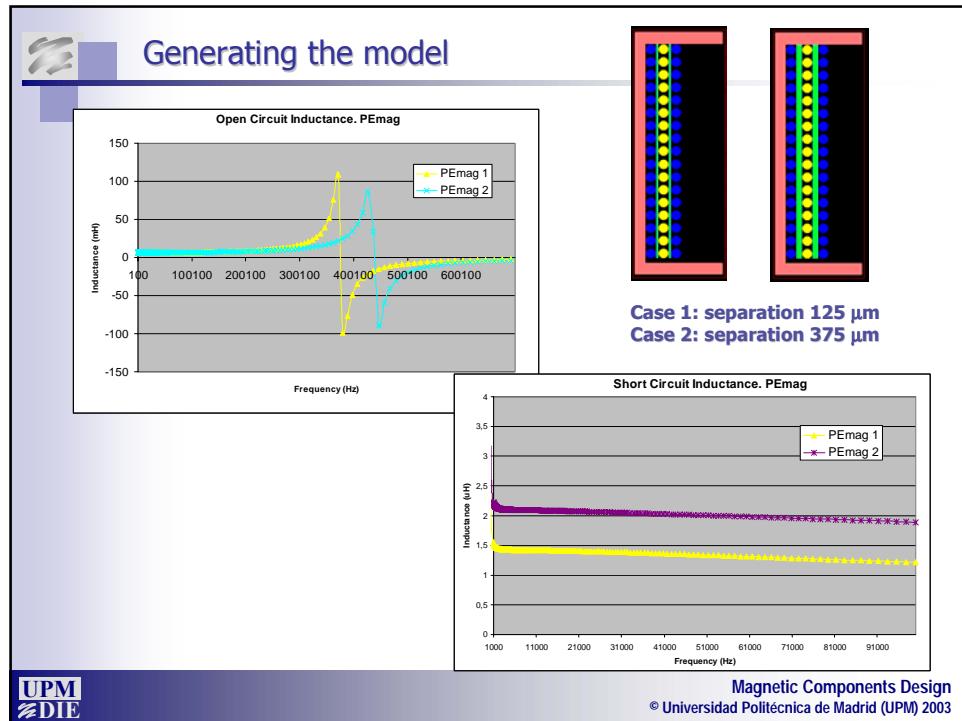
LF (< 1 skin depth)



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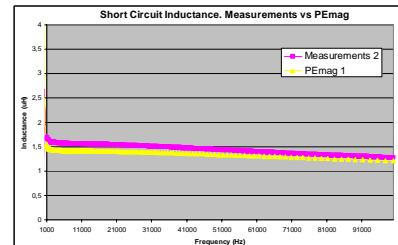
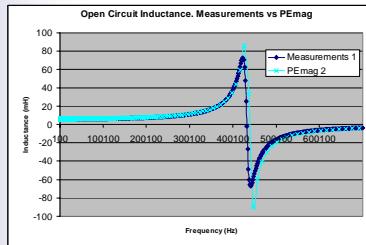




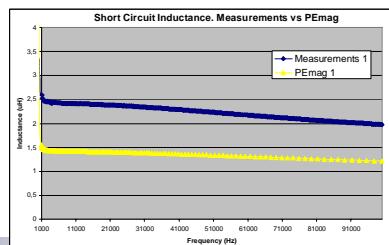
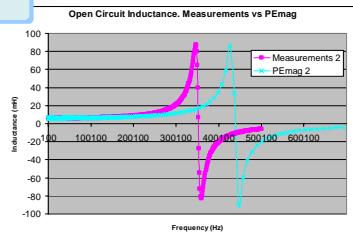


Comparing results

If only one real sample and only one model case are compared, results could be....



or....



Seminar Contents

- # Introduction
- # Basic Concepts
- # Design
- # Modeling
- # Simulation**
- # Virtual Prototyping Examples

Simulation

The diagram shows a flyback converter circuit with a primary voltage source E_1 , a PWM-controlled MOSFET, and a diode D_1 . The secondary side includes a voltage monitor VM_2 and a load. A waveform plot shows the primary current i_1 and secondary voltage v_2 over time. To the right is a schematic of a car's electrical system architecture, showing components like the engine, alternator, battery, and various sensors.

Entity

Architecture 1
Architecture 2
Architecture 3

```

package electrical_system IS
  SUBTYPE voltage IS real;
  SUBTYPE current IS real;

  NATURE electrical IS
    voltage ACROSS
    current THROUGH
    ground REFERENCE;
end package electrical_system;

```

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Simulation features

Simulation Goals

- Validation of the circuit operation
- Exploration of the waveforms
- Quantification of magnitudes (losses, stresses,...)
- Better understanding of the circuit operation

Simulation Challenges

- Lack of “accurate enough” models (Magnetic, Semiconductors, Layout...)
- Convergence problems (many “mathematical” parameters)
- Learning curve
- “Hard” transition from the design stage

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Simulator types

- # Circuit simulation (i.e. SPICE based)
- # System simulation (VHDL-AMS, MAST, SMD,...)

VHDL-AMS Code for a Resistor

```
ENTITY Resistor IS
  PORT (
    QUANTITY r : REAL := 1.0e+03; -- Default = 1 K
    TERMINAL p,m : ELECTRICAL);
END ENTITY Resistor;
```



```
ARCHITECTURE Rbehav1 OF Resistor IS
  QUANTITY voltage ACROSS current THROUGH p TO m;
BEGIN
  current == voltage/r;
END behav;
```



Seminar Contents

- # Introduction
- # Basic Concepts
- # Design
- # Modeling
- # Simulation
- # Examples

- ✓ Example 1: Coupling in Flyback transformer
- ✓ Example 2: Coupling in Multi-winding transformers
- ✓ Example 3: Multiphase Buck Inductors
- ✓ Example 4: Flyback transformer

Model
+
Simulation

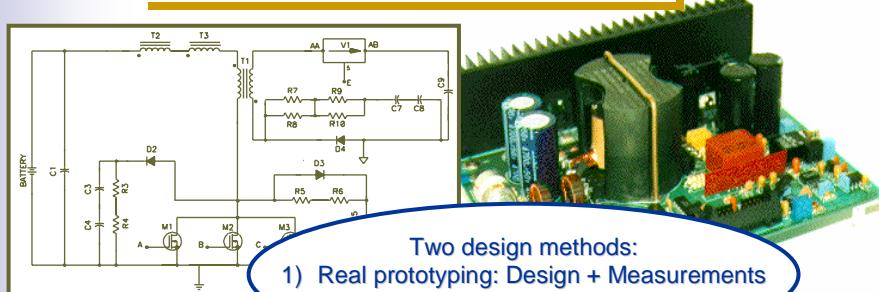
Analytical
vs
Numerical



Example 1: Coupling in Flyback Transformer

FLYBACK With Hysteretic Control

Capacitive Load: 0.5 F
 Output Voltage: 0 to 340 V
 Output Power: up to 1kW
 Input Voltage: 16 to 32 V
 Switching Frequency: 1kHz to 40 kHz
 Application: X ray equipment



Example 1: Flyback Converter

V_{ds} in MOSFET



Interleaving helps

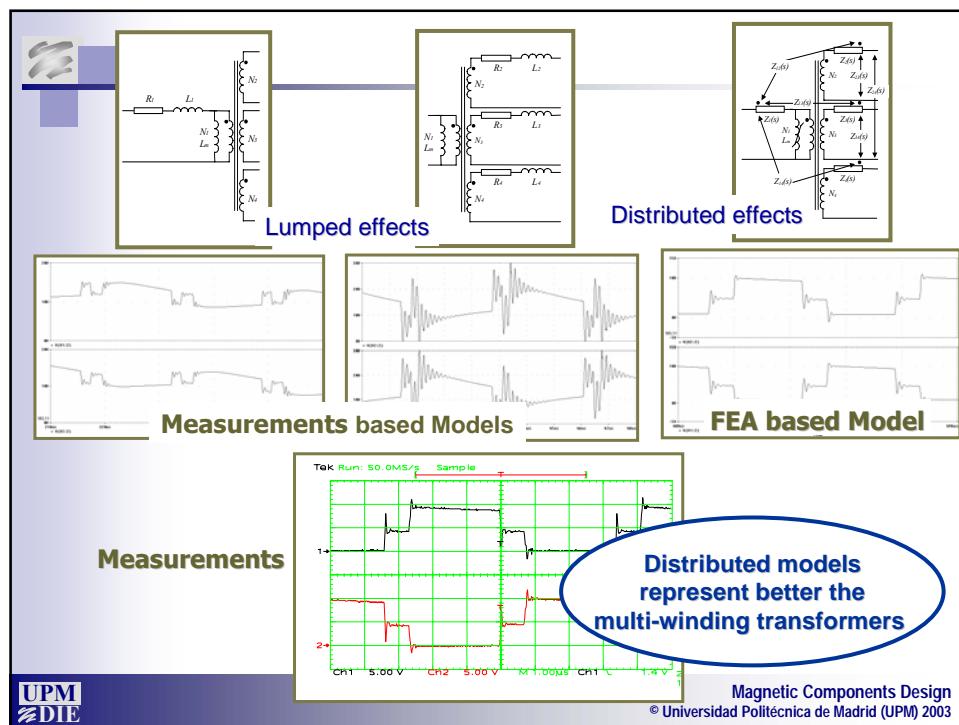
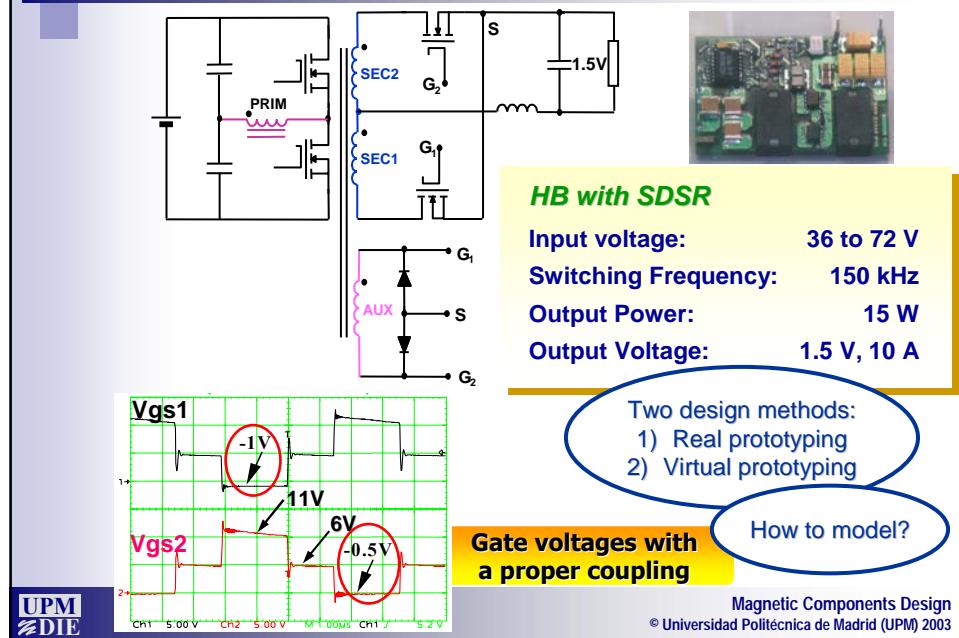
Transformer model
quantifies
(L_{LK})

110 V

220 V

Transformer model
+
Simulation
provides the impact on
the converter

Example 2: Coupling in Multi-winding transformers



How to select the proper winding Strategy ?

The diagram illustrates different winding strategies for a magnetic core:

- Single-winding:** Shows a core with one primary winding (PRIM) and one secondary winding (SEC).
- Multi-winding:** Shows a core with multiple primary (PRIM) and secondary (SEC) windings.
- Auxiliary winding:** Shows a core with a primary winding (PRIM), an auxiliary winding (AUX), and a secondary winding (SEC).
- Multi-winding transformers:** Shows a core with multiple primary (PRIM) and secondary (SEC) windings.
- Multi-output converters...**

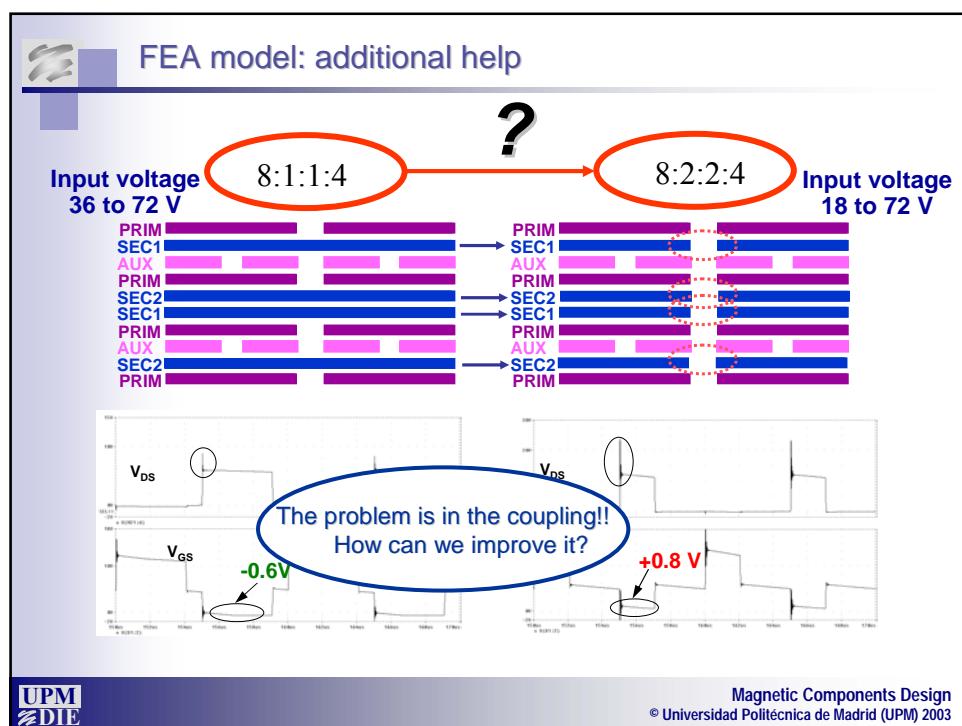
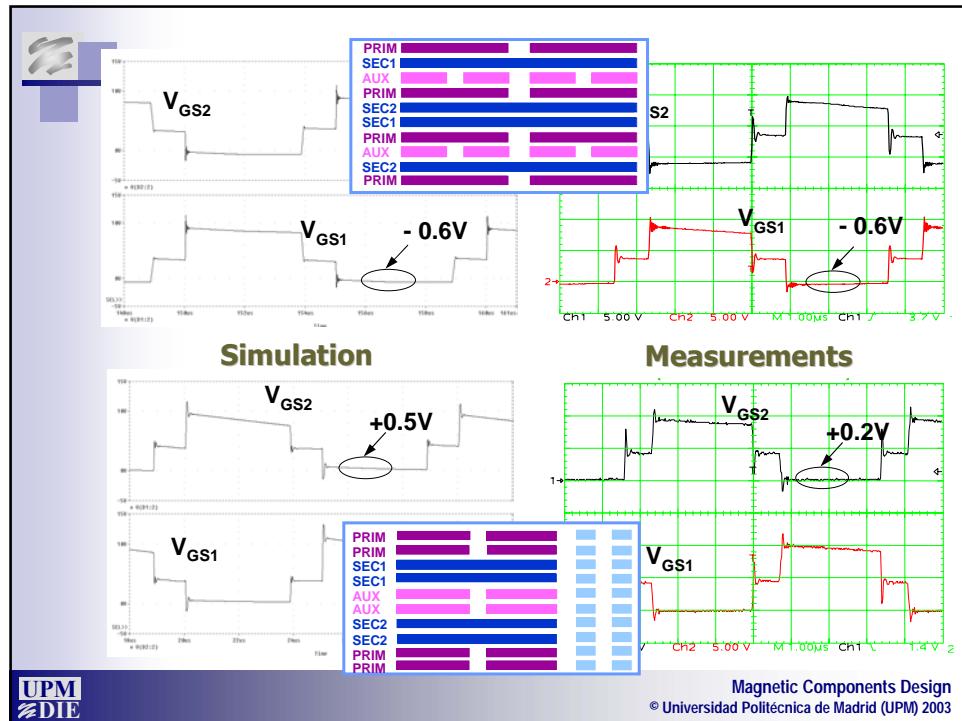
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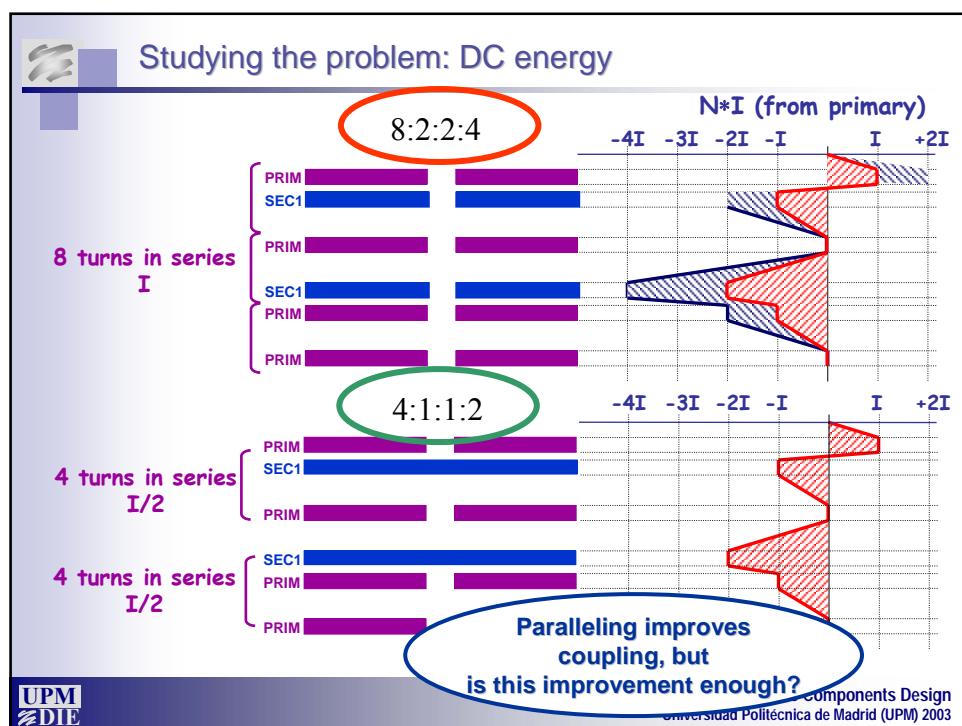
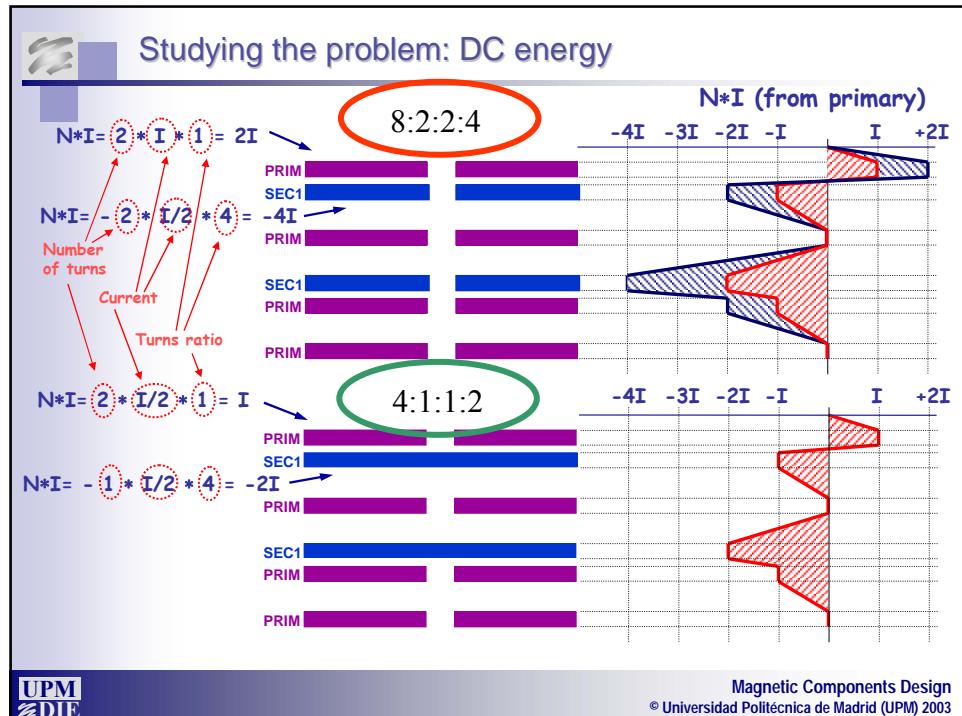
Using numeric (FEA) models

The diagram shows FEA results for different winding configurations:

- Auxiliary should be well coupled with primary:** A plot of V_{DS} vs time with an annotation: $+ 0.6V$.
- Losses, EMI:** A plot of V_{DS} vs time with an annotation: V_{GS} and $- 0.6V$.
- SWDSR works!!** A plot of V_{DS} vs time with an annotation: V_{GS} and $- 0.6V$.
- WORKS!!** A plot of V_{DS} vs time with an annotation: V_{GS} and $- 0.6V$.

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FEA model + simulation: additional help

8:2:2:4 4:1:1:2

PRIM SEC1 AUX PRIM SEC2 SEC1 PRIM AUX SEC2 PRIM

PRIM SEC1 AUX PRIM SEC2 SEC1 PRIM AUX SEC2 PRIM

Multi-winding transformers:
Interleaving in the proper way
Paralleling in the proper way

FEA models (distributed)
+ simulation
provide understanding
and can save time and cost

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Example 3: Multiphase Buck Inductors Automotive Application

Starter

Generator + Rectifier

36/42V

High power loads

36 V Battery

DC-DC

Low power loads

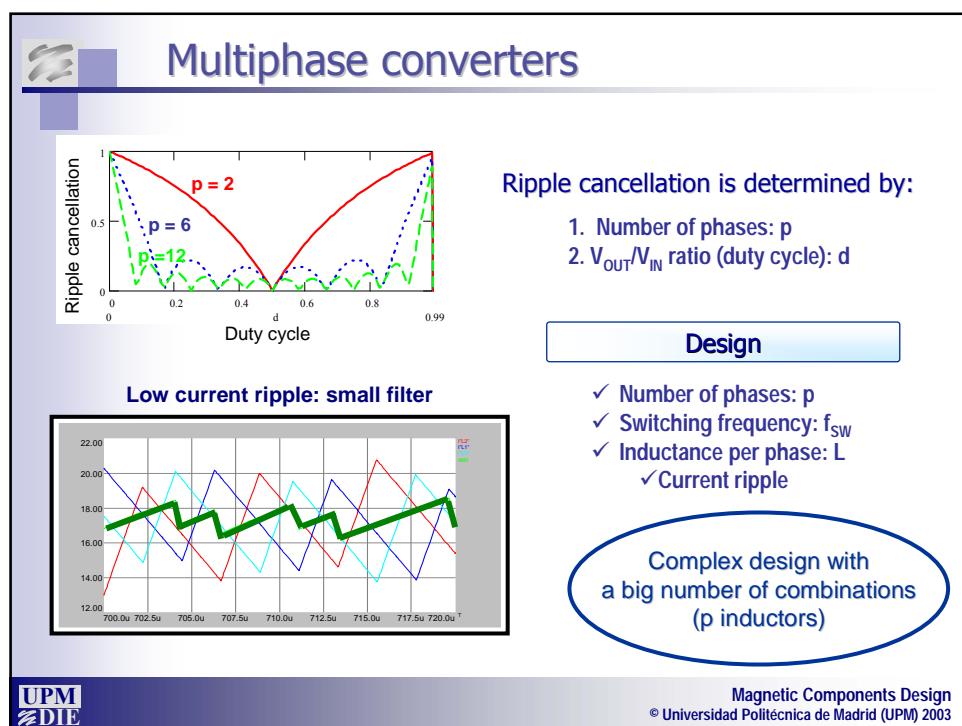
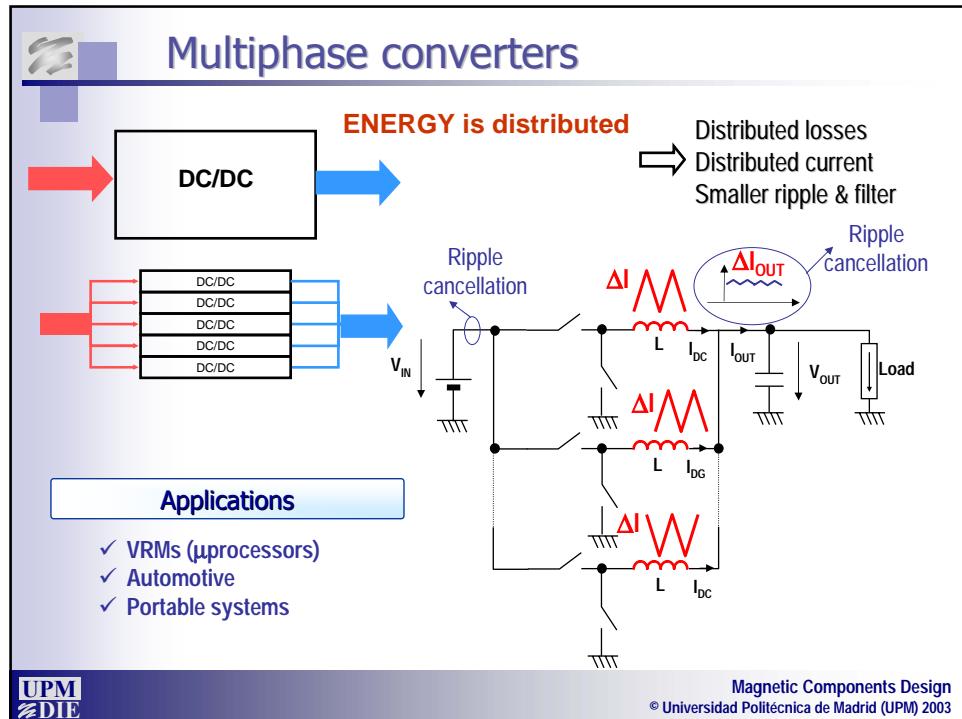
12/14V

12 V Battery

Magnetic design:
Analytical models fail!!!

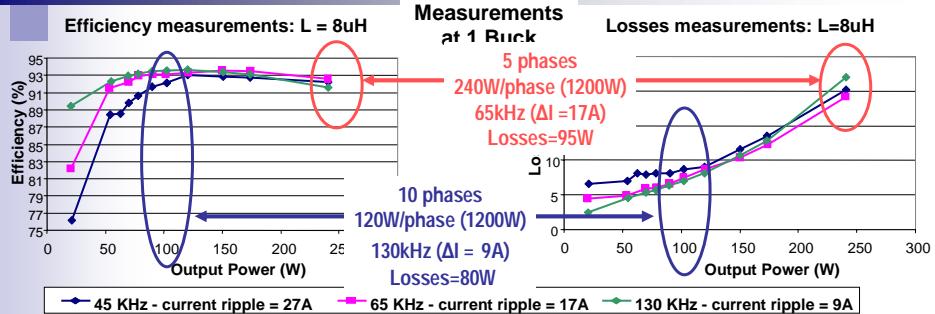
Direct fuel injection
Electric throttle valve control
Active suspension
42-V converter
Electrical assisted power steering
Steer-by-wire

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Which is the optimum number of phases?



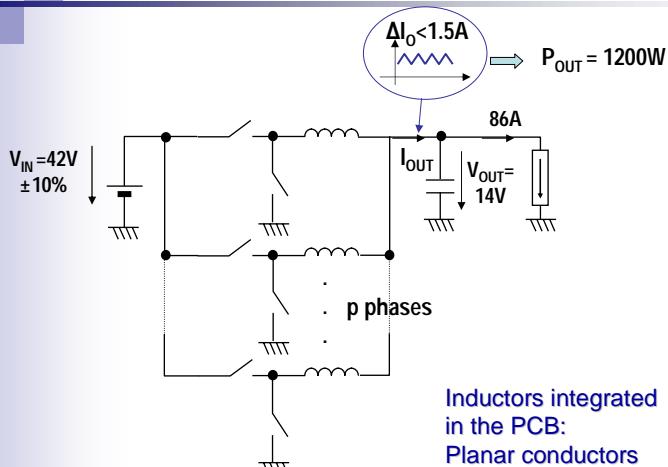
- Depending on I_{DC} /phase, or Power/phase, or Number of phases
the minimum losses are obtained at very different f_{sw}
- A high number of phases allows for a high f_{sw} with lower losses
Smaller inductor size per phase but high number of phases ⇒ Size?

Trade-off: size - efficiency



Converter specifications

Automotive application



Magnetics are 40%-60% of converter size

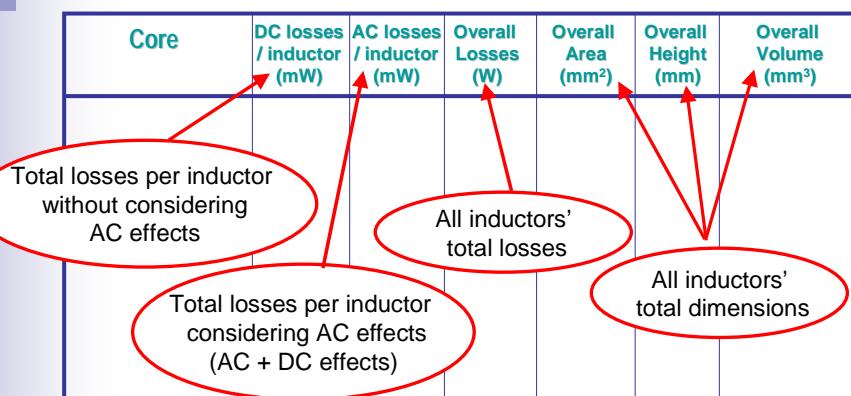
Design of inductors: analytical

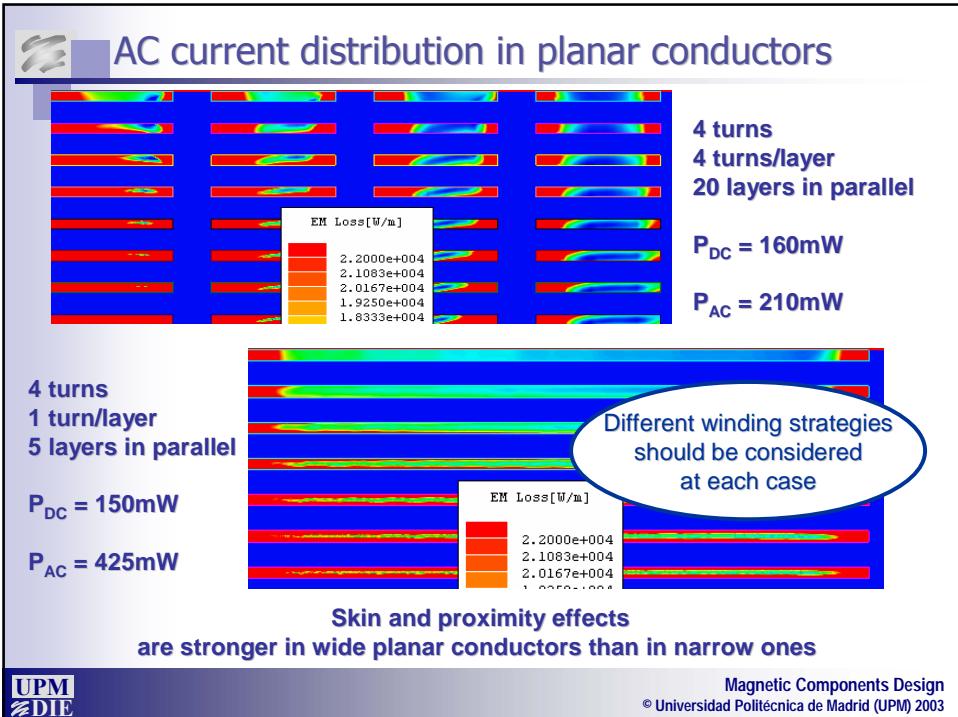
- ☒ Losses calculation accounts for:
 - ✓ DC resistance
 - ✓ Skin effect
 - ✓ Core losses ($P = k f^\alpha B^\beta$)
- ☒ Gap effect (2D) is not considered

Considered design options

Nº of phases	f_{sw} (kHz)	Cores	Material
6	100	RM6LP	3C90
10	200	RM7LP	3F3
16		RM8LP RM10LP RM12LP	3F4

Designs of inductors: 16 phases, $L=5\mu H$





Designs of inductors: 16 phases, $L=5\mu\text{H}$

Core	DC losses / inductor (mW)	AC losses / inductor (mW)	Overall Losses (W)	Overall Area (mm^2)	Overall Height (mm)	Overall Volume (mm^3)
Material Turns Winding strategy Gap						
16*RM7LP	420	425	6.8	5,010	9.8	49,000
16*RM8LP	275	285	4.5	6,300	11.6	73,125
16*RM10LP	90	155	2.4	9,660	13	125,600
Hundreds of combinations!!						
200kHz, $I_{DC} = 5.4\text{A}$, $\Delta I = 9.5\text{A}$						
16*RM6LP	250	300	4.9	3,550	9	31,970
16*RM7LP	215	235	3.7	5,010	9.8	49,000
16*RM8LP	130	150	2.4	6,300	11.6	73,125

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Designs of inductors: 10 phases, L=8μH

Core	DC losses / inductor (mW)	AC losses / inductor (mW)	Overall Losses (W)	Overall Area (mm ²)	Overall Height (mm)	Overall Volume (mm ³)
100kHz, $I_{DC} = 8.6A$, $\Delta I = 11.5A$						
10*RM7LP						
10*RM8LP	740	790	7.9	3,940	11.6	45,700
10*RM10LP	250	325	3.2	6,040	13	78,520
200kHz, $I_{DC} = 8.6A$, $\Delta I = 5.8A$						
10*RM7LP						
10*RM8LP	300	350	3.5	3,940	11.6	45,700
10*RM10LP	190	200	2	6,040	13	78,520

Designs of inductors: 6 phases, L=9.5μH

Core	DC losses / inductor (mW)	AC losses / inductor (mW)	Overall Losses (W)	Overall Area (mm ²)	Overall Height (mm)	Overall Volume (mm ³)
100kHz, $I_{DC} = 14.4A$, $\Delta I = 9.8A$						
6*RM10LP						
6*RM12LP	680	710	4.3	5,610	16.8	94,298
200kHz, $I_{DC} = 14.4A$, $\Delta I = 4.9A$						
6*RM10LP	735	760	4.5	3,625	13	47,110

Selected solutions based on analytical model

Solution	Overall Losses (W)	A (mm ²)	h (mm)	V (mm ³)
16 x RM7LP, 100kHz	6.8	5,010	9.8	49,000
16 x RM6LP, 200kHz	4.9	3,550	9	31,970
10 x RM8LP, 200kHz	3.5	3,940	11.6	45,700
6 x RM12LP, 100kHz	4.3	5,610	16.8	94,298
6 x RM10LP, 200kHz	4.5	3,625	13	47,110

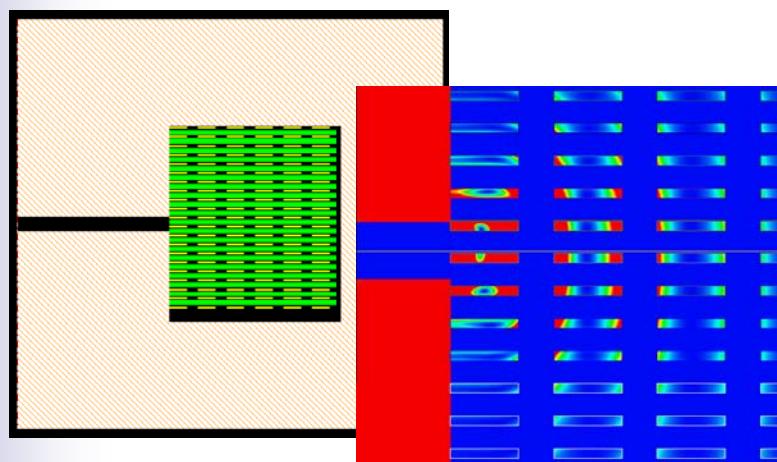
Final selection depends on:

- ✓ Losses of the whole converter
- ✓ Size of the whole converter.
Inductor size has a strong influence on overall size.
- ✓ Height requirements

Is the analytical model
good enough for this case?

Automotive application: gap effect

How does the gap affect the current distribution
and the losses of the selected solutions?



Automotive application: gap effect

Solution	Gap (μm)	ΔI /inductor (A)	Analytical model		FEA model	
			Losses /inductor (W)	ΔT in inductor ($^{\circ}\text{C}$)	Losses /inductor (W)	ΔT in inductor ($^{\circ}\text{C}$)
16*RM7LP, 100kHz	380	19	0.32	45	1.7	180
16*RM6LP, 200kHz	200	9.5	0.3	40	0.87	135
10*RM8LP, 200kHz	310	6	0.35	39	1.5	175
6*RM12LP, 100kHz	410	10	0.71	40	1.9	115
6*RM10LP, 200kHz	440	5	0.35	39	1.5	175

All the selected solutions based on analytical models are NOT FEASIBLE due to the gap effect!!!

Design of inductors: numerical (FEA) model

It accounts for:

- ✓ DC resistance
- ✓ Skin effect
- ✓ Proximity effect
- ✓ Gap effect
- ✓ Core losses

Considered design options

Nº of phases	f_{sw} (kHz)	Cores	Material
6	100	RM6LP	3C90
10	125	RM7LP	3F3
16	150	RM8LP	3F4
	200	RM10LP	
		RM12LP	



Design of inductor: 16 phases, 200kHz, RM7LP

	L (μ H)	ΔI / inductor (A)	ΔI_{OUT} (A)	Gap (μ m)	Analytical Losses / inductor (W)	Numerical Losses / inductor (W)
Material	2.5	19	1.2	170	0.28	2.2
Turns	3.6	13	0.8	215	0.22	2.0
Winding strategy	6.2	7.4	0.5	190	0.21	0.85
	9.4	4.9	0.3	260	0.33	0.63
	12.6	3.7	0.2	250	0.33	0.76

In this case, the optimum gap- ΔI combination is obtained for a small ΔI_{OUT} (0.3A)
The analytical model gives a very high $\Delta I = 13A$

This analysis is repeated for each selected case...



Feasible solutions: Numerical Model

5000 combinations analyzed!!!

From the point of view of the inductors:

Solution	ΔI_{OUT} (A)	Overall Losses (W)	Overall Area (mm ²)	Overall Height (mm)	Overall Volume (mm ³)
16 phases, RM7LP, 200kHz	0.3	10.1	5,010	9.8	49,000
16 phases, RM8LP, 125kHz	0.3	7.5	6,340	11.6	73,125
10 phases, RM10LP, 150kHz	1.2	6.9	6,040	13	78,520
6 phases, RM12LP, 125kHz	0.8	9	5,610	16.8	94,298

$\Delta I_{OUT} < 1.5A$

Virtual prototyping has allowed:

- ✓ To study 5000 cases, learning what is happening
- ✓ To obtain design rules
- ✓ To quantify and optimize

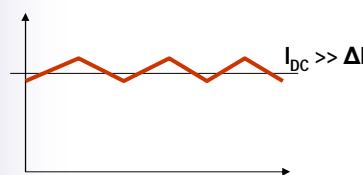




When are Analytical models useful?

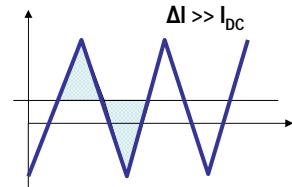
A

I_{DC} is predominant

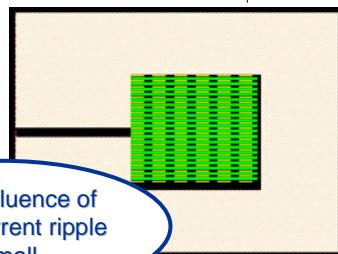


B

ΔI is predominant



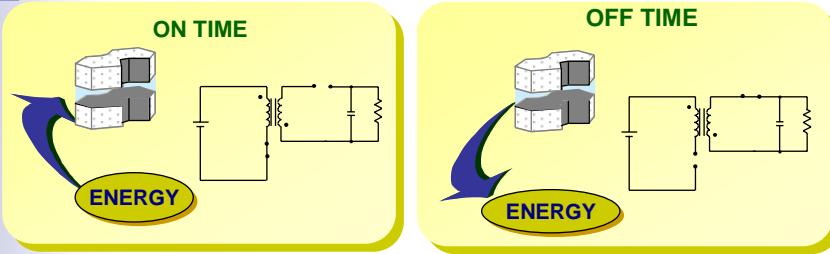
When influence of
Gap + current ripple
is small



Example 4: Flyback Transformer



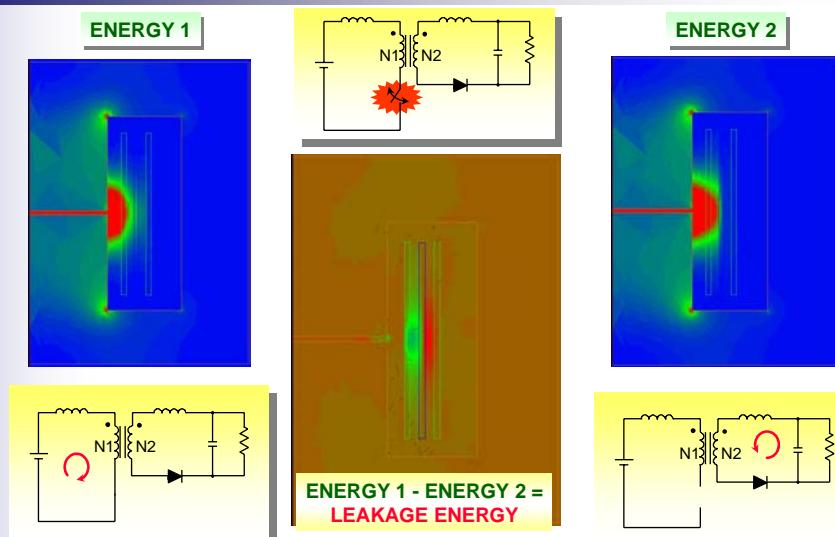
Electrical Description of Flyback Transformer



MAIN FEATURES

- Design in order to store energy
- Gap is usually needed
- Energy storage mainly in the gap
- Current is not flowing in both windings at the same time

Study of the fields: leakage inductance



Goal: minimization of this energy

Design example: Flyback

Transformer A
Analytical design

ETD 39, 3F3
Air Gap 2.2mm (86.6mils)
Primary
turns: 30
Wire Gauge: AWG22
(0.7mm, 27mils, 3 x skin depth)
Parallel: 3
Secondary
turns: 6
Wire Gauge: AWG22
(0.7mm, 27mils, 3 x skin depth)
Parallel: 18

Real prototyping: Design + Measurements

Gap and Leakage inductance NOT considered

Analytical results

- ✓ Core losses: 450mW
- ✓ Winding losses: 200mW
- ✓ $\Delta T = 7^\circ\text{C}$

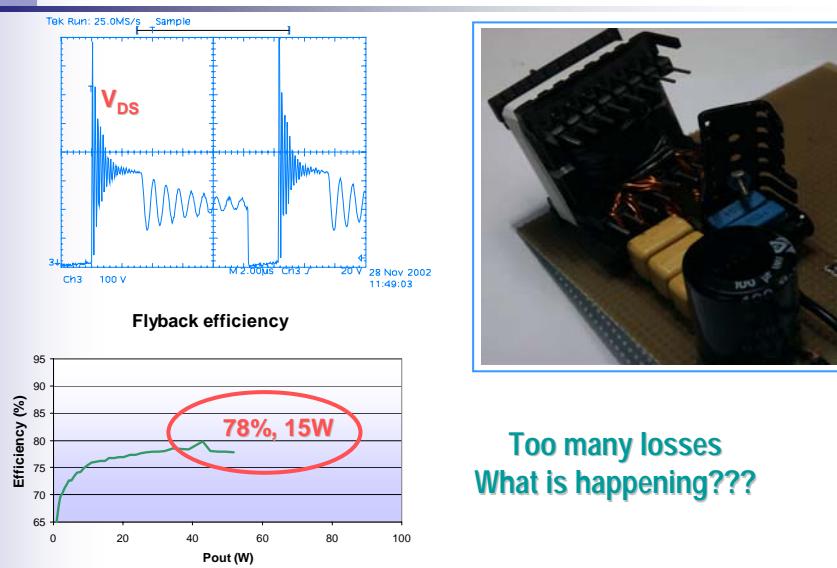
DC resistance Skin effect Core losses

High window filling

UPM DIE

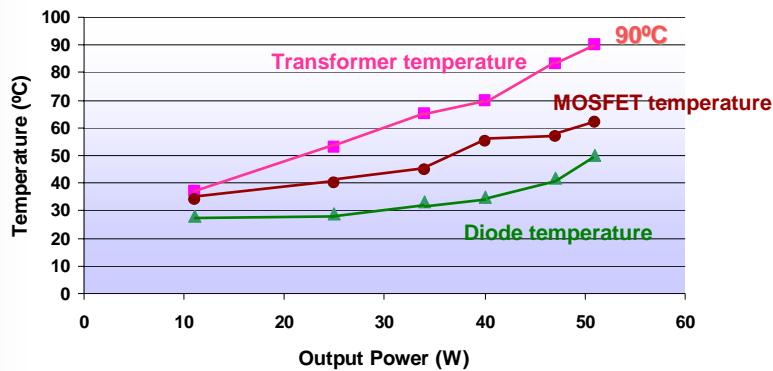
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Transformer A: Measurements on Flyback prototype





Transformer A: Measurements on Flyback prototype



The hottest component is the transformer, full power (100W) can not be achieved due to the transformer losses



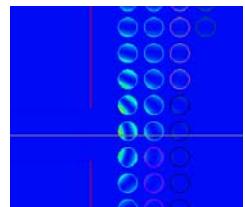
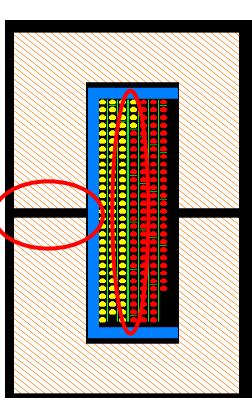
What can we do?



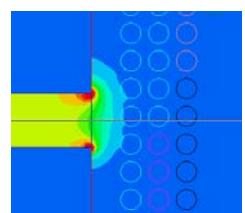
Impact of the air gap effect?
Impact of the leakage inductance?

Virtual prototyping:
Numerical Model (FEA)

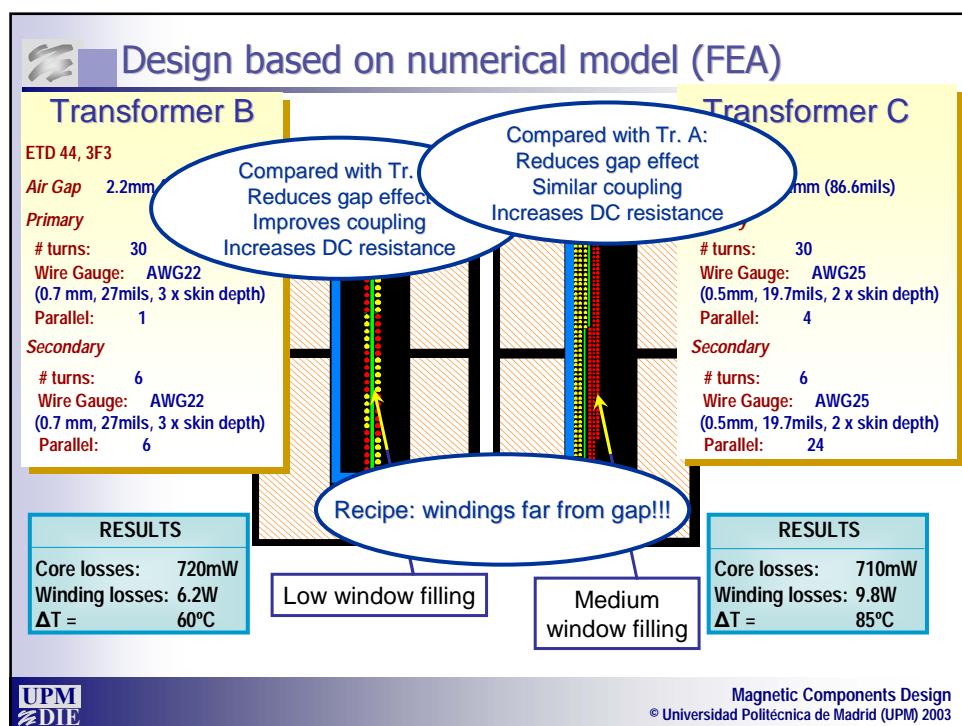
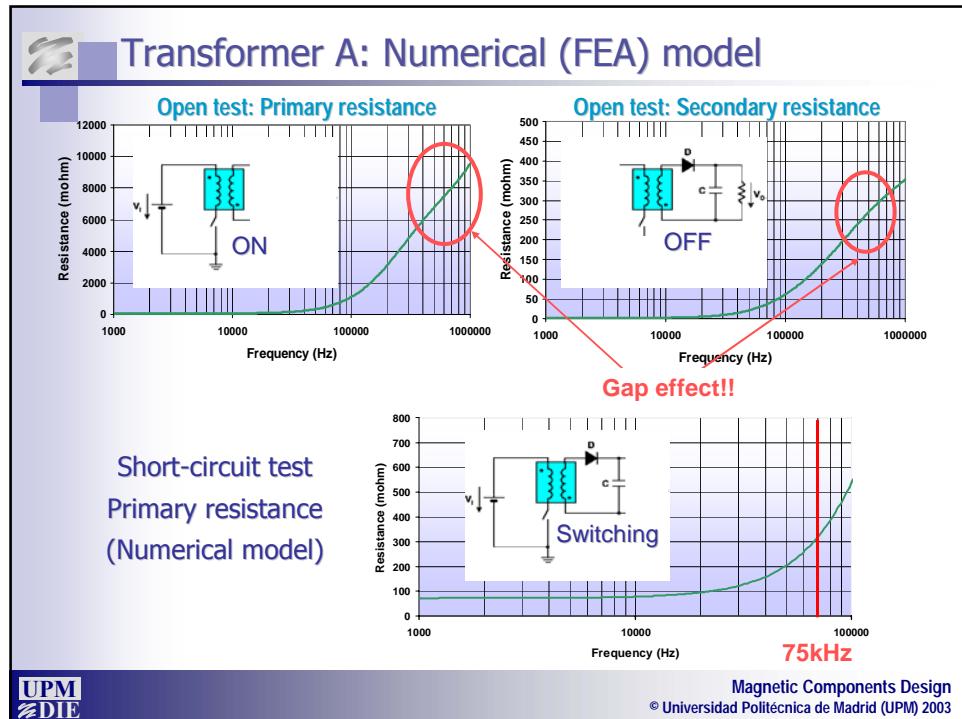
Core losses: 460mW
Winding losses:
11W!!!
 $\Delta T = 140^\circ\text{C}$



Current density

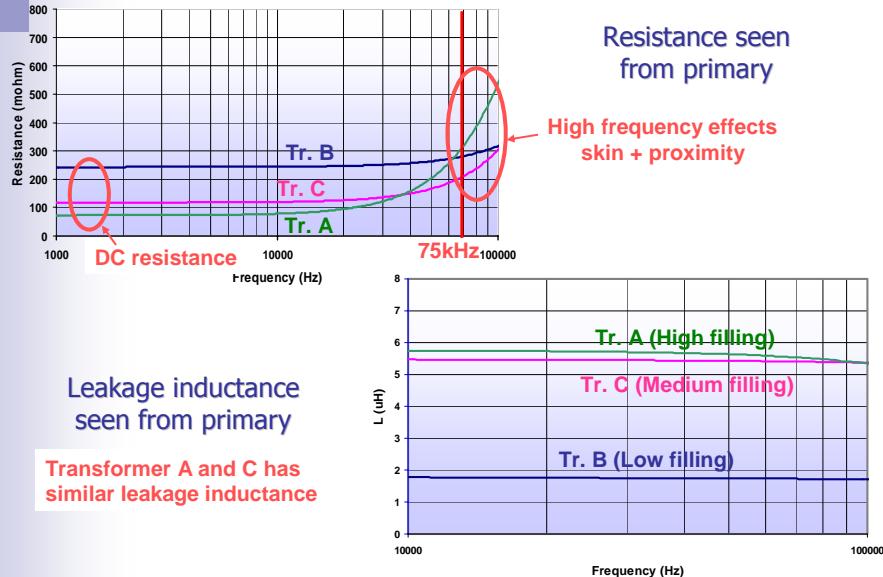


Energy density

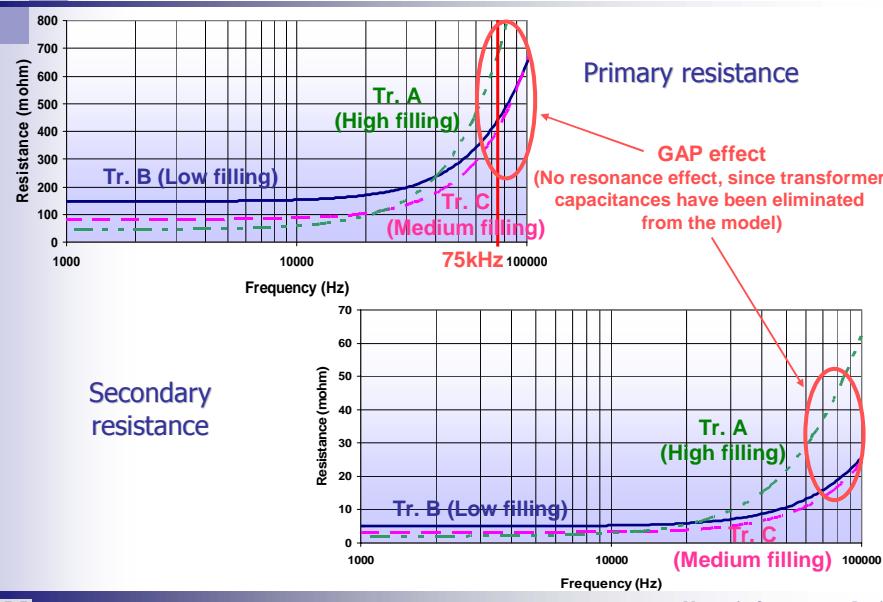




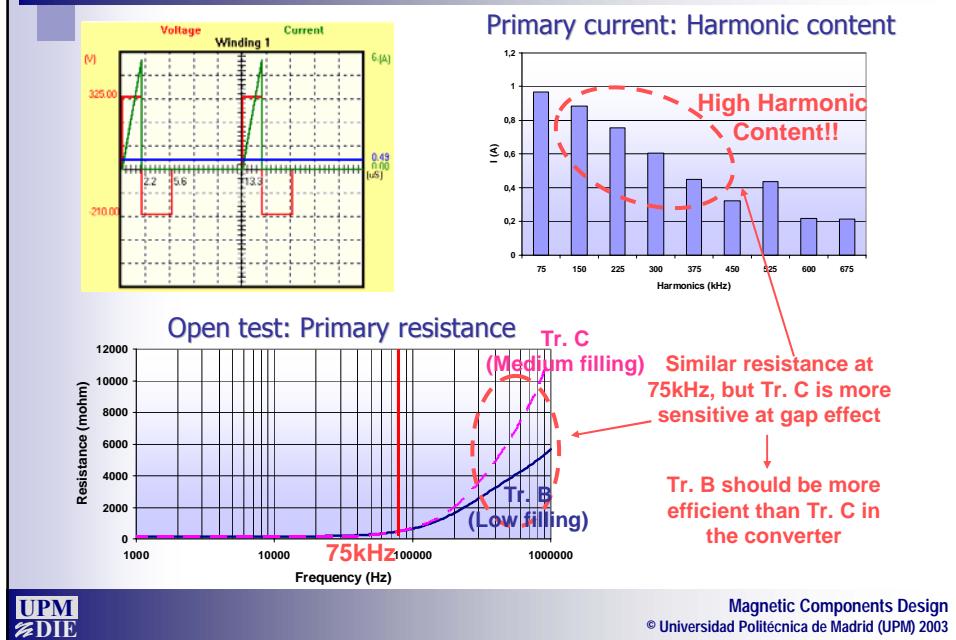
Numerical (FEA) models: short-circuit test



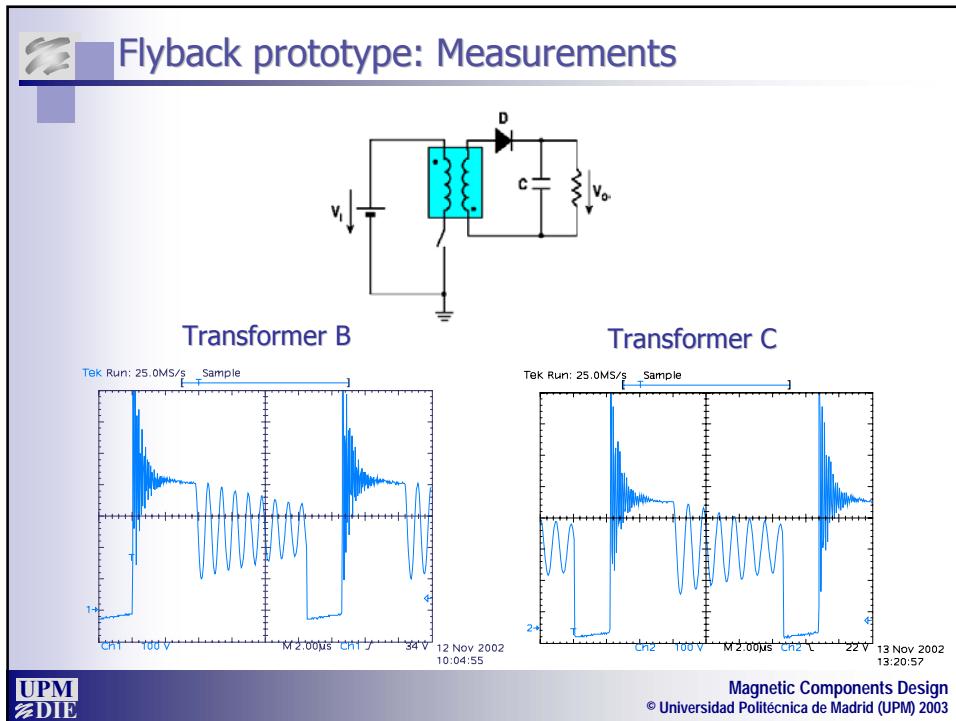
Numerical (FEA) models: Open test



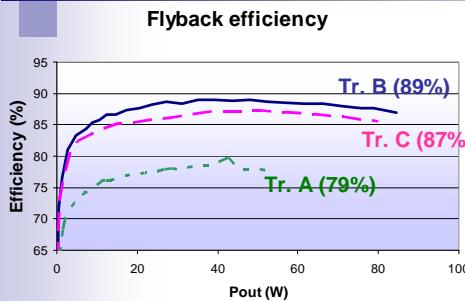
Studying the problem



Flyback prototype: Measurements

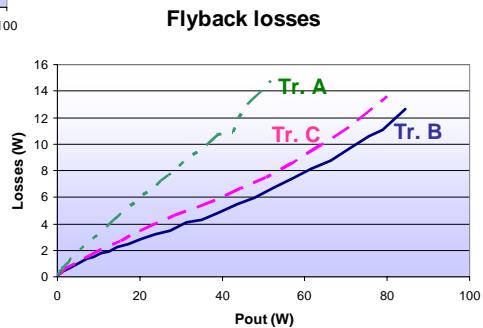


Flyback prototype: Measurements



Transformer A and C has similar inductance, however converter losses are very different \Rightarrow GAP effect!!

Losses with Transformer C are 27% higher (3W higher) than with Transformer B



Virtual prototyping accounts for 2D effects:

- ✓ problems can be properly understood
- ✓ optimum designs can be proposed:
 - ✓ Not too many wires but properly placed and winded



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Real Prototyping

- Simple
- Accuracy
- Cost
- Time

Feasible!!

Virtual Prototyping

Proper Model

Understand Quantify

Simulation

Impact on converter
Detect problems

Re-design

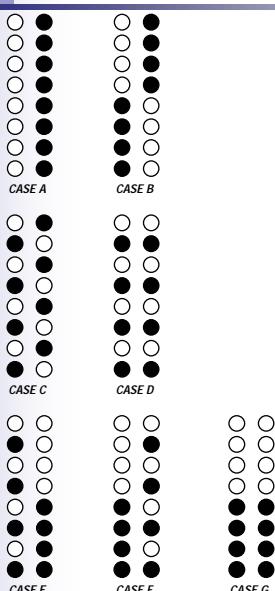


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Interleaving

Comparison of winding strategies



Case	$L_{\text{leakage}} (\mu\text{H}) @ 200\text{kHz}$	$L_{\text{leakage}} (\mu\text{H}) @ 2\text{MHz}$
A	0.475	0.248
B	0.432	0.231
C	0.130	0.087
D	0.276	0.185
E	4.144	2.827
F	4.239	2.857
G	13.979	9.496